Inspectors or Google Earth? Optimal fiscal policies under uncertain detection of evaders

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- Unrealistic assumption: detection rates vary between 30% (Erard and Feinstein, 2009) and 50% (Feinstein, 1991).

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 - Theoretical consideration.
 - Empirical issue: governments invest resources to improve their tax administration's capacity to detect evaders.

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- This is precisely the purpose of our paper.
- We characterize these optimal investments and we show how they interact with other dimensions of an optimal fiscal policy.

• The model

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- Numerical simulations of the model

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- Conclusion

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- Presents two class of active agents: individuals, government.

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 - $\theta \in [0, 1]$: fraction of dishonest (rich) taxpayers.

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- q_i : consumption of the (numéraire) private good
- g : public good.
- The strictly increasing and concave utility function u satisfies

$$u(0) = 0$$
 $\lim_{q \to 0} u_q = \infty$ $\lim_{q \to \infty} u_q = 0.$

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- The government designs the fiscal policy...
- but delegates its implementation to a tax administration.

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- Second stage: the government designs the tax law (t, π, f)
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 - The tax law has to verify taxpayers' ex-post limited liability, horizontal and vertical equity.

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- With all revenues collected (taxes and fines, net of investment and audit costs), the government finances the public good g.

The model: detection technology

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- $\nu > 0$: investment productivity.

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- First stage: we find the optimal level of investment $\hat{\kappa}$.

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- Mookherjee and Png (1989): no need to audit a taxpayer that reported to be rich→ π_p.
- The optimal tax law solves the following problem

 $\begin{cases}
Max \\
t_{p}, t_{r}, f_{r,p}, \pi_{p,g} \\
subject to \\
0 \le \pi_{p} \le 1 \\
t_{p} \le y_{p} \\
t_{r} + f_{r,p} \le y_{r} \\
u(y_{r} - t_{r}) \ge (1 - \delta \pi_{p}) u(y_{r} - t_{p}) + \delta \pi_{p} u(y_{r} - t_{r} - f_{r,p}) \\
g = \mu t_{r} + (1 - \mu) t_{p} - (1 - \mu) \pi_{p} c - \kappa
\end{cases}$ (B) (LL_p) (LL_r)

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Second stage: the no audit regime

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- In this case, there is no complete revelation of individual types.
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- The government solves

$$\begin{aligned} & \underset{t_p, t_r, g}{\text{Max}} \quad \mu \left[(1 - \theta) u(y_r - t_r) + \theta u(y_r - t_p) \right] + (1 - \mu) u(y_p - t_p) + g \\ & \text{subject to} \\ & g = \left[1 - \mu (1 - \theta) \right] t_p + \mu (1 - \theta) t_r \end{aligned}$$

Second stage: the optimal tax law

Let $\underline{\delta} \leq 1$ be the threshold that characterizes when each regime emerges.

Stage



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 - **(**) We find κ^A : the level of investment that maximizes $\mathbb{E}W^A$.
 - Provided both regimes of audit emerge, we compare $\mathbb{E}W^A(\kappa^A)$ with $\mathbb{E}W^{NA}(0)$.

 \bullet Under the audit regime, the optimal investment κ^A solves the following problem

$$\begin{split} & \underset{\kappa}{\text{Max }} \mu \left[u(y_r - t_r^A) + t_r^A \right] + (1 - \mu) \left[u(y_p - t_p^A) + t_p^A \right] - (1 - \mu) \pi_p^A c - \kappa \\ & \text{subject to} \\ & \delta = \delta(\kappa, \nu) \\ & \max\{0, \underline{\kappa}\} \leq \kappa \\ & \kappa \leq \mu t_r^A + (1 - \mu) t_p^A - (1 - \mu) \pi_p^A c \end{split}$$

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 - Existence of a solution

- Under the audit regime, the optimal investment κ^A solves the following problem
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 - Existence of a solution
 - Characterization of a solution
 - The constraint set may be empty.
 - As the expected welfare $\mathbb{E}W^A$ is not generally concave, the first-order conditions are useless to completely characterize the maximum.
 - The comparison between $\mathbb{E}W^{NA}$, $\mathbb{E}W^{A}(\kappa^{A})$ and $\mathbb{E}W^{FA}(\kappa^{FA})$ is not straightforward because it is a comparison of levels.

Numerical simulations of the model

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- Taxpayers are characterized by a CRRA utility function

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• The detection probability function $\delta(\kappa, \nu)$ is formalized as a logistic

$$\delta(\kappa,\nu) = \delta_{\iota} + \nu \frac{1 - e^{-\frac{\kappa}{a}}}{1 - ne^{-\frac{\kappa}{a}}},$$

where a = 0.235 and n = 0.99.

PARAMETER	DEFINITION	BASELINE VALUE
σ	Coefficient of relative risk aversion	0.71
μ	Percentage of rich taxpayers	67
y _r	Income of the rich	\$52.304
Уp	Income of the poor	\$6.747
θ	Percentage of dishonest taxpayers	36
С	Cost of a single audit	\$14.833
δ_{ι}	Initial detection probability	0.4
ν	Investment productivity	0.225

All money values are in thousands of dollars.

SOLUTIONS	WITHOUT INVESTMENT	WITH INVESTMENT
$\widehat{\kappa}$	0	\$0.059
$\widehat{\delta}$	0.4	0.62 (+55%)
\widehat{t}_p	\$6.03	\$5.83 (+2.9%)
\hat{t}_r	\$44.35	\$47.4 (+6.9%)
IP	-0.087	0.176
$\widehat{\pi}_{p}$	1	0.89 (-11%)
ĝ	\$26.81	\$30.58 (+14.06%)
EPS	85.3%	85.5% (+2.4%)

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- Improvements in the investment productivity generate better results, in quantitative terms, than improvements in the initial detection probability.
- The public good's provision and the efficiency of the public sector increase with investment.

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- We simulate the model to identify the solutions but also to study how the optimal investment interacts with the other components of the optimal fiscal policy.
- Clearly this model suggests that one needs to incorporate such investments into the currently used definitions of 'tax effort' in empirical models.