

Valuing Unpaid Tax Assessments: Estimating Long-Run Collectability Using an Econometric Approach

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Introduction

The Government Management Reform Act of 1994² and the Chief Financial Officers (CFO) Act of 1990³ made the Government Accountability Office (GAO) responsible for annual audits of agency-wide financial statements and the U.S. government's consolidated financial statements. As of Fiscal Year 2016, there were 400 billion dollars in unpaid assessments (UA) the IRS has the authority to collect.

There are four financial classifications of UA inventory assets. For this paper, just like in the financial statements, the memo financial classification will be excluded, as the assessments in this inventory are not true receivables. It does not meet any of the other financial classifications as it contains fraudulent/frivolous tax returns and multi-year examinations with global netting issues. The remaining classifications are:

- **Taxes receivable**—assessments that the taxpayer has agreed to, or there has been a legal determination of liability;
- **Compliance assessments**—unagreed enforcement assessments; and
- **Write-offs**—amounts deemed to have little collection potential, but by statute must remain on the books for the length of the collection statute (usually 10 years).

The IRS reports on its financial statements an estimated dollar amount it expects to collect from the taxes receivable portion of the unpaid assessments inventory. Obtaining a clean GAO audit rests in part on the accuracy of the UA collectability estimate. In this paper, we develop an econometric approach to estimating the value of unpaid assessments inventory. This approach is data-driven and provides a more comprehensive estimate of the value of the entire inventory of unpaid assessments over the life of each asset.

Unpaid Assessments and Collectability Estimates

While a major component of the IRS's mission is assessing and collecting the proper amount of tax, the challenge for IRS financial management is to accurately account for and determine the net realizable value of an ever-increasing inventory of unpaid assessments. This can be challenging in an environment with increasingly limited resources. The IRS has long sought a more flexible decision tool that could strengthen its financial reports and reconcile reports to downstream collection activities driven by an individual debtor's characteristics.

Unpaid assessments consist of taxes, penalties, and interest that have not been collected or abated. IRS CFO staff are responsible for estimating, reconciling, analyzing trends, and preparing projections on the unpaid assessment inventory. These tasks require personnel to evaluate taxpayer account information over time to identify those characteristics that impact the probability of collections. Reconciliation of balances to unpaid assessment information reports ensures the integrity of the financial statements.

¹ The views and opinions presented in this paper reflect those of the authors. They do not necessarily reflect the views or the official position of the Internal Revenue Service.

² Civic Impulse. (2017). S. 2170—103rd Congress: Government Management Reform Act of 1994. Retrieved from <https://www.govtrack.us/congress/bills/103/s2170>.

³ Chief Financial Officers (CFO) Act of 1990 (1990, Nov). Public Law 101-576, 101st Congress. Retrieved from <http://www.gao.gov/special.pubs/af12194.pdf>.

Federal accounting standards (FASAB 7) require reporting Federal taxes receivable net of allowance for loss on taxes receivable on the balance sheet and notes to the financial statements, and the disclosure of compliance assessments and write-offs in the supplemental information to financial statements.⁴ New requirements for the accounting of expected credit losses are set forth in IFRS 9 (International Financial Reporting Standard) and take effect for large banks' 2018 financial statements.⁵ Accounting principles in the U.S. have evolved over the last 80 years, but they are still considered to be more rules-based in their approach to accounting standards and may not address unforeseen issues that arise in the normal course of business. Some government entities including the U.S. Postal Service, U.S. Department of Treasury entities, and smaller executive and legislative branch entities continue to apply this rules-based FASB (Financial Accounting Standards Board) approach. Principles-based standards, such as Generally Accepted Accounting Principles (GAAP) from the FASAB, provide more flexible applications to a broad range of situations.⁶ More than 100 countries have adopted IFRS to some degree. FASAB now requires a loss allowance based on the expected losses over the life of the assets.

The recovery model-based approach presented in this paper supports the process of estimating recovery of taxes receivable with the corresponding allowance for loss (loss given default). Scores developed from the models provide an opportunity to automate and enhance the annual financial statement audit by reducing the inherent risk associated with small sample designs, thereby helping to ensure the IRS receives an unqualified (clean) opinion.

For most unpaid assessments, the statutory period for collection is 10 years. During the statutory period, changes in economic conditions, tax law, tax administration policy, and resources devoted to tax administration can potentially affect the actual collection from some assets. The current method for estimating the value of unpaid assessments involves conducting intensive reviews of a sample of the inventory to determine collectability. The IRS currently uses subject-matter experts to confirm that the assessments are classified properly in the sample, calculates the value of the taxes receivable portion of the sample, and then projects potential collection to the taxes receivable population of the entire UA inventory. This figure is reported in the IRS financial statements as the net realizable value of the UA inventory.

Under the current sampling method, the accuracy of the reported UA inventory amount relies heavily on the subject-matter expert's classification of the assessments in the sample. This process is very labor intensive. The fact that the process relies on the financial classification poses an inherent risk. If programming changes are made in the IRS business systems that are not reflected/recognized in the financial systems, UA assets could be misclassified. When assessments are misclassified in the audit sample, that error is projected to the population estimate. This can put the IRS at risk of not obtaining a clean audit opinion on its financial statements from GAO. In addition, the method does not value assets where the taxpayer has not agreed with the IRS's assessment or those that have been moved into a "Write-off" financial classification. Furthermore, this method does not account for policy and economic changes potentially affecting collectability over the life of the asset.

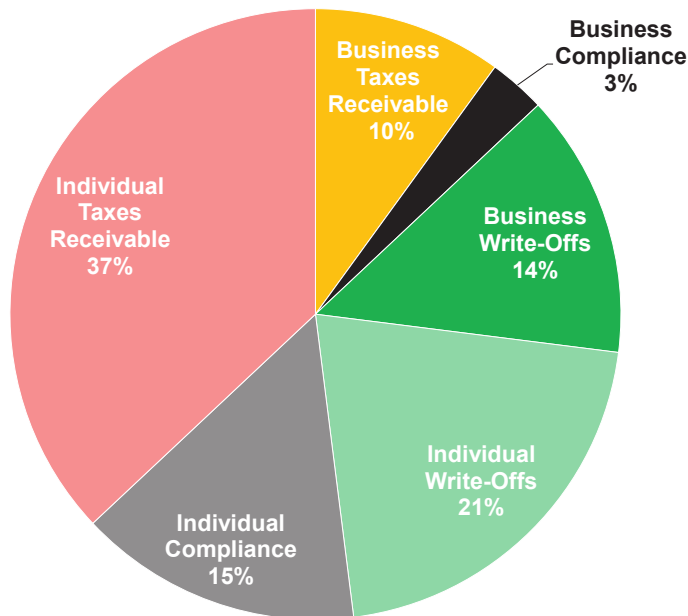
Figure 1 shows the composition of the FY 2016 unpaid assessments by financial classification. Taxes receivable assets are 47 percent of the UA inventory. The current sample method for valuing UA does not account for the potential collectability of the remaining 53 percent of unpaid assessments that are classified as either write-offs or compliance assessments.

⁴ Federal Accounting Standards Advisory Board (FASAB).

⁵ GPPC (2016)

⁶ <http://www.fasab.gov/appropriate-source-of-gaap/>.

FIGURE 1. Composition of the Total \$400 Billion of Gross Unpaid Assessments



SOURCE: Custodial Detail Database (CDDb) as of September 30, 2016, Individual Master File and Business Master File extract cycle 201637.

Objective

In this research, we develop a predictive model to determine the net realizable value of each unpaid assessment at any point in time. The model enables us to estimate the proportion of the current balance that will be recovered over its remaining life. We define “recovery” as the total net payments to be realized in the future as a percentage of the current module balance. The model estimates the amounts to be collected against the current balance of each UA asset based on an estimated proportion that will be recovered.

Research Design: Recovery Model

Overview

We use a logistic model to estimate the recovery rate—the proportion of the current unpaid balance that will be paid over the remaining life of the statute. The data are compiled from the IRS Compliance Data Warehouse (CDW) Unpaid Assessments data, referred to as ARDI (Accounts Receivable Dollar Inventory) in the CDW. We pool repeated January cross sections of the inventory from 2004 to 2014. We compile annual net payments from 2002 to 2016. The models provide scores or estimates of the percentage of the current balance the IRS can expect to recover on each asset in the Individual and Business Master File unpaid assessment inventory. A two-step modeling approach is used to statistically control for cases where all potential payments are not observed. These controls allow us to back out the impact of only partially observing payment streams on some assets, thus allowing a “full statute” payment/recovery estimate. Eight model specifications are created, based on the Master File Tax Class of the unpaid assessments assets.

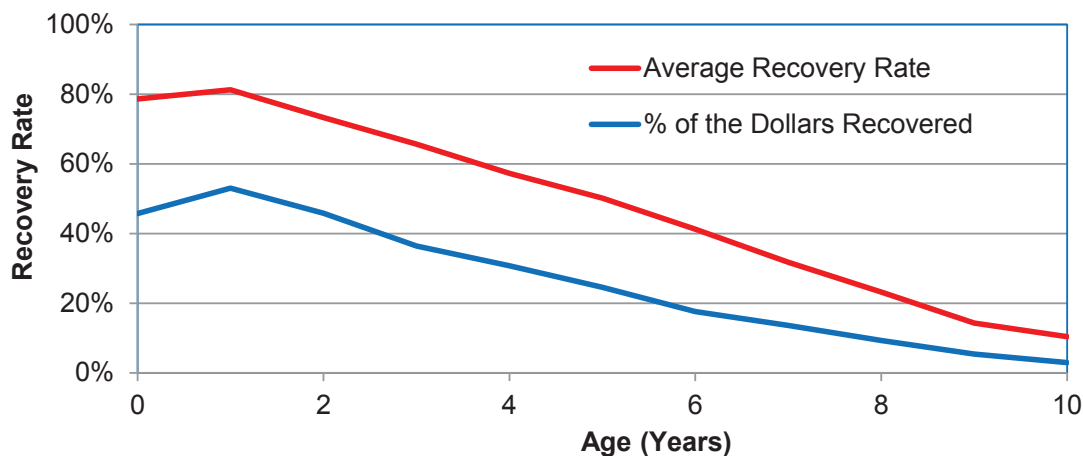
Data Dilemma: Incomplete Payments vs. Data Currency

Most UA assets have 10-year statutes, and at any point in time the UA inventory contains assessments from multiple years. Unless you go back in time more than 10 years, there will be a proportion of cases where all the potential payments are not observed. This creates a data dilemma. Typically, the most recent data are more relevant for prediction because they reflect today’s economic, resource, and policy situations. However, looking at inventories further back in time allows for more cases where all the payments have been observed.

Also, having multiple years of UA inventory allows for more variation in the mix of cases and business cycle fluctuations.

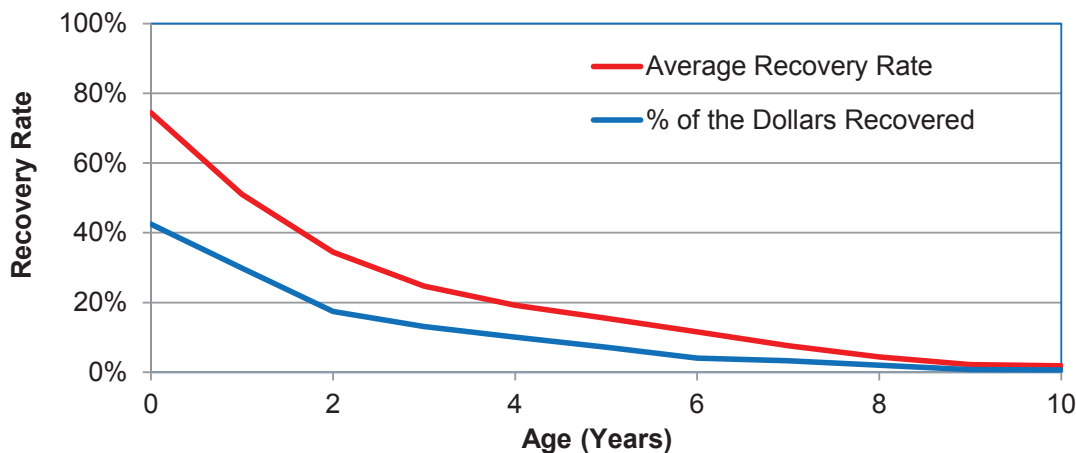
Figures 2 and 3 show recovery rates by the age of the assessment for Form 1040 and Form 941 (respectively) for the January 2015 UA inventory. In general, the recovery rates for both forms are lower for older assessments. The decay in recovery rate is much slower for individuals than for businesses. These trends reflect the fact that many assessments are resolved early in the collection process. Assessments that are 10 years old make up a smaller proportion of UA collections compared to younger cases for both individual and business tax classes. Over time, debt becomes less collectable, and less collectable debt tends to get older. Both facts contribute to the lower observed recovery for older debt.

FIGURE 2. Recovery Rate for the 2005 Inventory of Individual Master File Form 1040 Unpaid Assessments



SOURCE: Compliance Data Warehouse, Unpaid Assessment Entity and Module information, Unpaid Assessment inventory as of January 2005, net payments on the associated modules 2005–2015.

FIGURE 3. Recovery Rate for the 2005 Inventory of Business Master File Form 941 Unpaid Assessments



SOURCE: Compliance Data Warehouse, Unpaid Assessment Entity and Module Information, Unpaid Assessment inventory as of January 2005, net payments on the associated modules 2005–2015.

The recovery model needs to account for the truncated payments observed for the most recent UA assets to properly model the relationship between time and asset collectability. This truncation is more difficult to account for because the data are a repeated cross section of UA inventory. As such, separate logistic models were used to approximate the likelihood that all the potential payments are not observed by the end of the sample period. The predicted probability is included in the recovery model as a control for payment truncation on recovery estimates. In addition, we include a control for time remaining on the collection statute at the end of our sample.

Controlling for Unobserved Payments

An asset has unobserved payments when at the end of our sample period the case is still in UA and the observed recovery is less than 100 percent. Future payments can and do exceed the current balance in many cases since interest and penalties will continue to accrue. The first-stage model is designed to calculate the probability of unobserved payments on an asset.

Let $T=1$ if the above conditions are met and zero otherwise. Then model T as:

$$\text{Prob}(T=1) = \frac{e^{Z\alpha}}{1 + e^{Z\alpha}},$$

where Z contains variables in X (defined below) and year dummy variables. These annual dummies control for the timing of the observations and thus how long payments can be observed. This functional form provides probabilities for the payment stream being truncated. We include this probability in the recovery model as an additional explanatory variable to control for assets having unobserved payments.

Recovery Model

Consider the following basic recovery model form:

Let P_t be the net payments made during a year on an unpaid assessment module and B_n be the current total module balance, then define the variable Y as:

$$Y = \frac{\sum_{t=n}^{10} P_t}{B_n}.$$

Then let $R = \text{Max}(Y, 1)$.

Then, the estimated recovery model becomes:

$$X_t \beta = \beta_0 + \beta_1 \ln(\text{Module Balance}) + \beta_2 \ln(\text{Entity Balance}) + \beta_3 \text{Age} + \beta_4 \text{Age}^2 + \beta_5 (\text{Net Payment in Prior Year/Module Balance}) + \dots$$

$$+ \beta_p (\text{Probability of not observing all payments})$$

$$+ \beta_T (\text{Time Remaining on the statute at the end of the sample}).$$

We can then model recovery, R , as

$$\text{Estimated Recovery} = R = F(X\beta) = \frac{e^{X\beta}}{1 + e^{X\beta}},$$

where $F(\cdot)$ is a cumulative logistic distribution function. The nonlinear logistic regression model will provide the expected recovery, ranging between zero and one, on each asset given the asset's array of characteristics, X .

For a "full statute" estimate of recovery, we set:

- The probability of not observing all payments = 0 and,
- Time remaining on the statute at the end of the sample = 0.

As previously mentioned, separate models and calculations are estimated for individual and business tax classes. The dependent variable "recovery" is defined as total net payments in the future as a percentage of the current balance. Recovery is considered as 100 percent when the accumulated payments exceed the current balance. Payments are not discounted based on when they are received.⁷ The model generates an estimated recovery percentage that ranges from 0 to 100 percent.

The models control for measures of the taxpayer's income, number of unpaid assessment modules the taxpayer has in UA inventory, the age of the assessments, payments in each of the prior 2 years, and current location and status in the collection process. The models also control for major source of assessments and transaction category, financial classification, previous filing compliance, and type of taxpayer.

Estimated value is then calculated as the expected percent recovered multiplied by the current balance. This estimates the dollar amount the IRS expects to collect from the balance today over the remaining life of the asset. Unlike the sample method that produces estimates for only taxes receivable assets in UA inventory, the recovery models produce estimates for all assets regardless of financial classification.

Results

The results for separate model specifications were estimated for the various Individual and Business tax classes/form types. Table 1 shows the parameter estimates for the variables used to control for truncated payments in the models: "probability of truncated payments" and "time remaining at the end of the sample." In all but one instance, the "probability of truncated payments" estimates are positive and "time remaining at the end of the sample" estimates are negative. Thus, these controls work in opposite directions when the variables are set to zero in the full statute estimate calculation. This at first would seem counter-intuitive. However, the estimates are the result of pooling multiple cross sections of data over multiple years, each with different periods of time to observe payments. The more time remaining to observe payments at the end of the sample, the larger the adjustment that occurs to the estimated recovery rate. However, that adjustment is counterbalanced by the likelihood that the payments are truncated. This probability is related to the collectability of the case. So, for a given cross section of data, observations that are less collectible get a smaller "bump" in estimated recovery. That bump will vary in the sample depending on the yearly cross section from which the case originates.

Estimates from GAO audit samples show collections have nearly doubled (\$26.3 billion to \$49.2 billion) from 2008 to 2016, far outpacing the rate of growth in adjusted taxes receivable (\$124.3 billion to \$178.4 billion).⁸ Figure 4 shows the model predicted average and actual observed recovery rates and recovered dollars for the Individual Income Tax Form 1040 UA inventory in Calendar Years January 2004 through 2016. In Figure 4, actual observed dollars collected on individual income tax UA are shown at nearly 30 percent, declining for more recent years because in these years, collections on more recent assets have not yet been realized. The difference between the estimated dollar recovery rate and the observed dollar recovery rate illustrates the effect of payment truncation. The more constant rate shown in the estimated dollar recovery line is the result of estimating the yet-to-be observed collections on the newer assets. More information on the predictions is provided in the appendix. This effect is shown by the increasing percent-truncated line over time. As more cases have truncated payment streams, the actual and estimated get further apart. If we don't back out the impact of the truncation, the predicted rates tend to follow the observed.

⁷ The current UA valuation process does not make any attempt to account for the timing of payments.

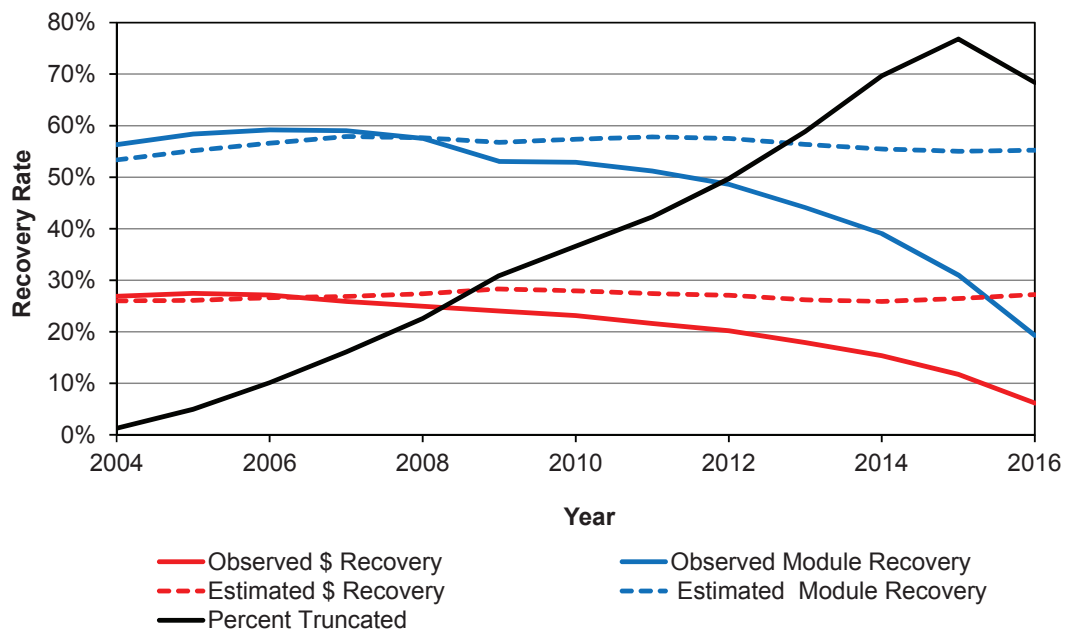
⁸ U.S. Government Accountability Office (GAO) (2016, November), various years.

TABLE 1. Recovery Model Payment Truncation Control Parameter Estimates*

| Form Number/Issue | Probability of Truncated Payments | Time Remaining at the End of the Sample |
|-----------------------------|-----------------------------------|---|
| Form 940 | 2.732 (0.022) | -1.916 (0.013) |
| Form 941 | 2.232 (0.011) | -1.125 (0.003) |
| Form 1040 | 0.791 (0.009) | -0.776 (0.002) |
| Form 1065 | 1.350 (0.025) | -1.327 (0.012) |
| Form 1120 | 1.770 (0.035) | -0.999 (0.007) |
| Trust Fund Recovery Penalty | -0.456 (0.015) | -0.601 (0.003) |
| Business Other | 1.330 (0.014) | -1.214 (0.006) |
| Individual Other | 0.198 (0.084) | -0.616 (0.019) |

NOTE: All estimates are significant at the 5% level. Standard errors reported in parentheses.
SOURCE: CFO Unpaid Assessments Inventory Recovery Model Output.

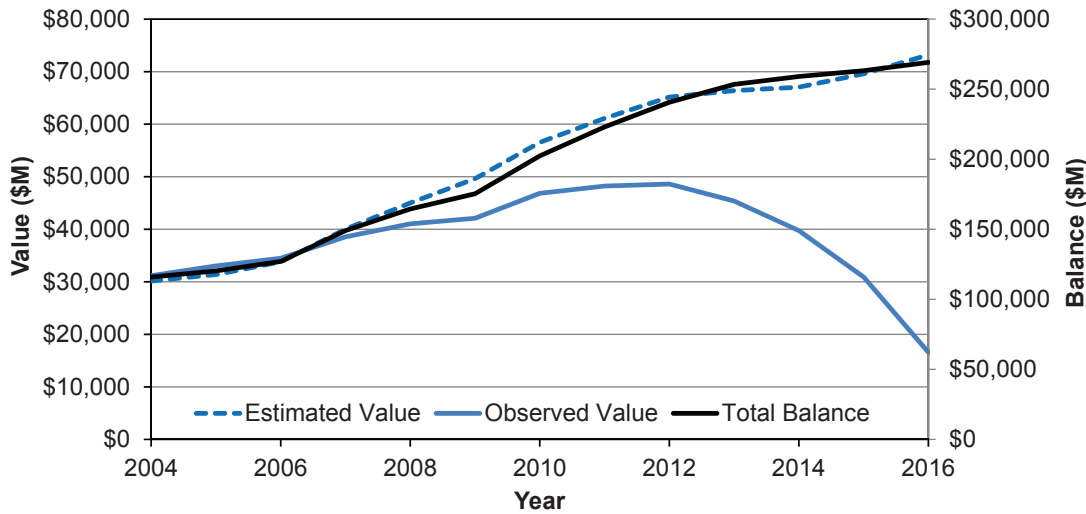
FIGURE 4. Individual Income Tax Form 1040—Average Percent of Modules and Dollars Recovered, Model Full-Statute Estimates and Actual Observed to Date



SOURCE: Form 1040 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

GAO audit results include net realizable values in the aggregate, whereas the recovery model approach can break out subpopulations by any form type. Figure 5 shows that the estimated value for Form 1040 assets tracks very closely to the total module balance for this population. The difference between the observed and estimated value is the truncation effect as stated before; the impact of the yet-to-be-made payments on the more recent assets over time not being currently observed. This is consistent with the recovery rates observed in Figure 2.

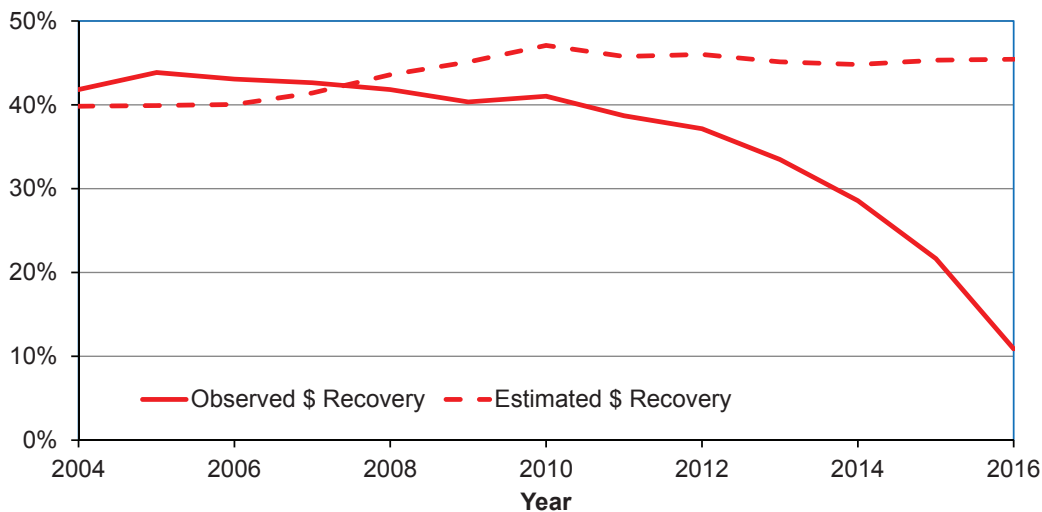
FIGURE 5. All Forms 1040—Aggregate Value and Module Balance



SOURCE: Form 1040 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

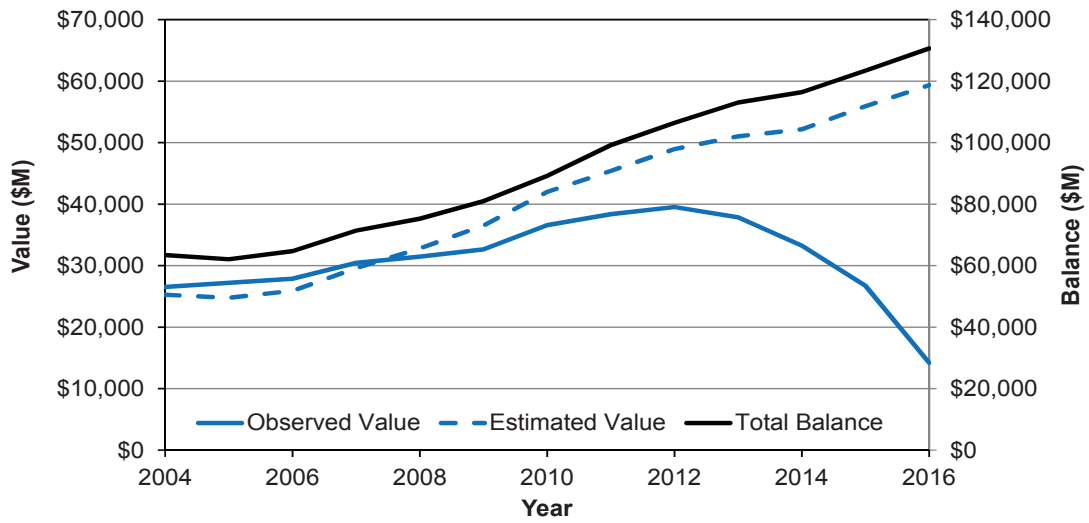
Figures 6 and 7 show the model estimates and observed actuals for the taxes receivable portion of Form 1040 UA inventory. These figures show higher average estimated recovery and actual observed rates than Form 1040 UA inventory. The taxes receivable recovery rates are higher than the total Form 1040 UA recovery rate because comparatively fewer payments are received on compliance assessments and write-offs. In Figure 7, the taxes receivable estimated value tracks the total module balance for Form 1040 taxes receivable.

FIGURE 6. Observed and Estimated Recovery Percentages of Form 1040 Modules—Taxes Receivable



SOURCE: Form 1040 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

FIGURE 7. Form 1040 Aggregate Value and Module Balance—Taxes Receivable

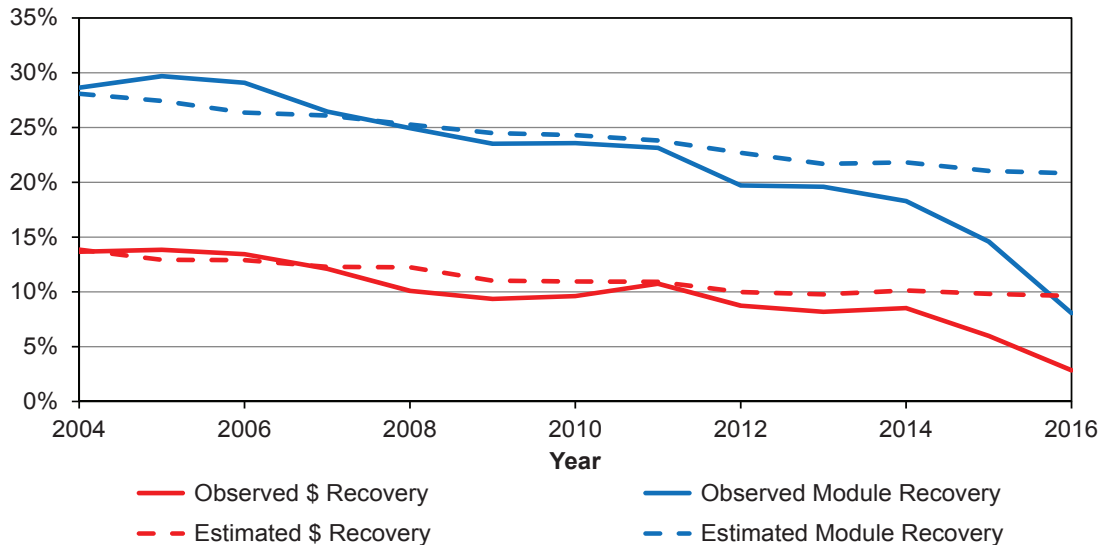


SOURCE: Form 1040 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

Figure 8 shows the model predicted average and actual observed recovery rates and recovered dollars for the business tax Form 941, *Employer’s Quarterly Federal Tax Return*, UA inventory in Calendar Years January 2004 through 2016. Employers use this form to report income taxes and Social Security or Medicare taxes withheld from employees’ paychecks, and to pay the employer’s portion of Social Security or Medicare tax.

The recovery rates for the Form 941 UA inventory displayed in Figure 8 are lower and decrease at a faster rate than Form 1040 UA recovery rates. Actual observed dollars collected on Form 941 business tax UA is shown at nearly 14 percent, declining for more recent years as collections on more recent assets have not yet been realized. Like with Form 1040 UA, the difference between the estimated dollar recovery rate and the observed dollar recovery rate illustrates the truncation effect. The more rapid drop in recovery rates can be explained by the fact that business entities become “defunct” more frequently than individuals. As companies go out of business the payments on unpaid assessments may stop. As such, it takes fewer years to observe most of the payments, making the impact of truncated payments less pronounced for business tax UA inventory.

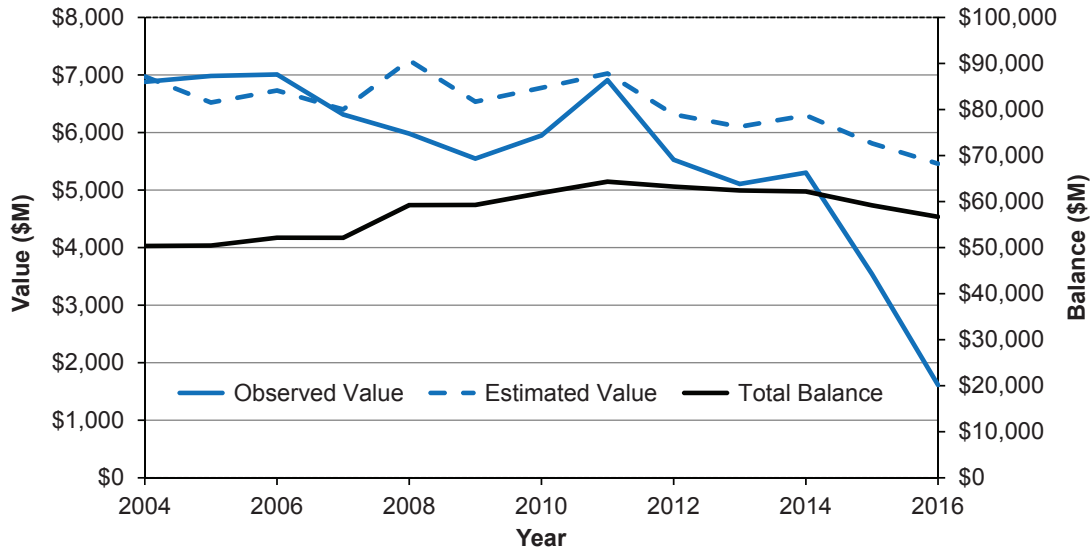
Figure 8. All Forms 941—Average Percentage of Modules and Dollars Recovered



SOURCE: Form 1040 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

In Figure 9, there is very little growth in the balance and a general decline in the value of the assets relative to the balance for Form 941 UA. The estimated value however does move with the actual value and declines.

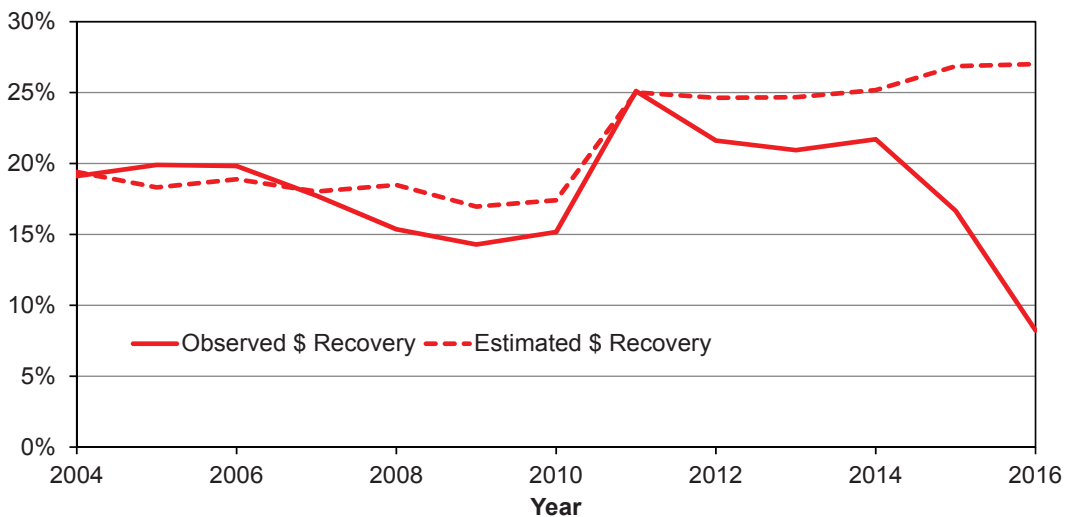
FIGURE 9. All Forms 941—Aggregate Value and Module Balance



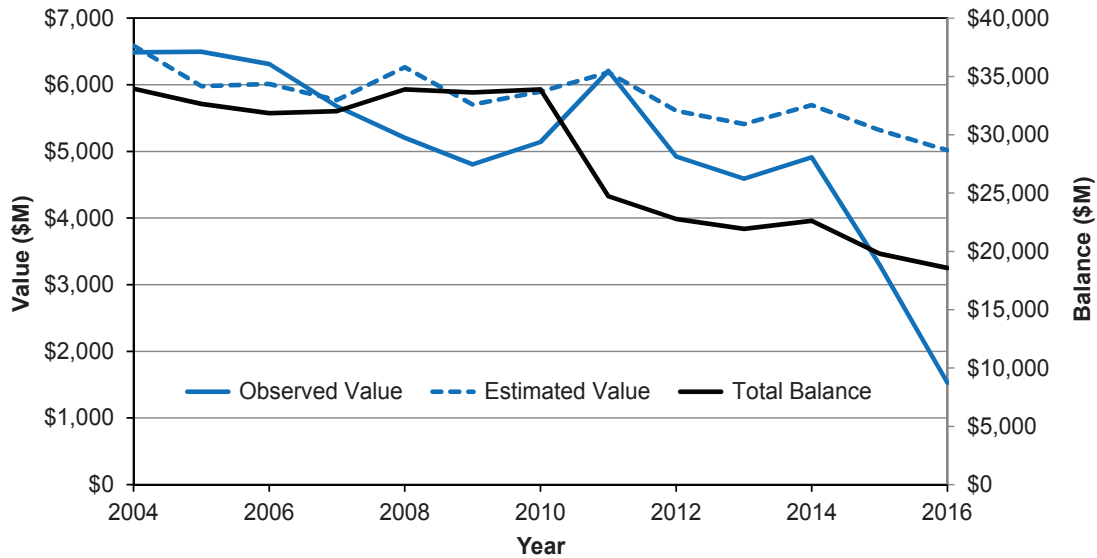
SOURCE: Form 1040 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

Figure 10 shows the dollar recovery rates for the taxes receivable portion of the Form 941 UA. From 2004 to 2016, the estimated recovery ranges from 19 to 26 percent. There is a noticeable jump in the rates, both estimated and observed for 2011. The value and total balance are reported in Figure 11. The estimated Form 941 UA value (black line) has fluctuated and declined from \$6.5 billion to approximately \$5 billion, and appears to move with the observed value. There is also a large decline in the aggregate balance (dashed line) from nearly \$34 billion to \$18.5 billion. This decline is proportionally larger than the decline in the value. There was a portion of the UA inventory that moved from taxes receivable to write-off. However, the model estimates were already heavily discounting these assets even before they moved to write-off. Thus, the estimated value does not decline.

FIGURE 10. Observed and Estimated Recovery Percentages of Form 941 Modules—Taxes Receivable



SOURCE: Form 941 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

FIGURE 11. Form 941 Aggregate Value and Module—Taxes Receivable

SOURCE: Form 941 Unpaid Assessments Inventory Recovery Model Results. Compliance Data Warehouse Accounts Receivable Dollar Inventory 2004–2016.

Conclusions

In this paper, we develop a predictive model of collectability for unpaid tax assessments. The primary role of this model is to provide an objective methodology for valuing UA that does not require time-intensive sampling and the inherent risks of financial misclassification. To predict the value of the inventory of unpaid assessments, we compile a repeated cross section of the UA inventory over multiple years. This allows us to capitalize on variation in the make-up of UA. However, it does introduce a unique truncation issue because of the pooling of the cross sections. We employ two statistical controls to account for this censoring.

The models will improve the objectivity of financial management reporting and eliminate sampling errors, thereby improving the precision of the IRS financial statement audit. The entire inventory of UA can be continuously rescored and valued, with little resource costs. Explanations for changes in the aggregate value of UA can easily be traced back to changes in the inventory and the associated case characteristics.

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Appendix

TABLE A1. Form 941 Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 38% | 38% | 38% | 1% | \$33,950 | \$6,486 | \$6,588 |
| | 2005 | 41% | 39% | 38% | 1% | \$32,640 | \$6,495 | \$5,977 |
| | 2006 | 44% | 41% | 41% | 3% | \$31,839 | \$6,311 | \$6,013 |
| | 2007 | 40% | 43% | 40% | 9% | \$32,016 | \$5,677 | \$5,771 |
| | 2008 | 40% | 45% | 42% | 20% | \$33,878 | \$5,204 | \$6,262 |
| | 2009 | 39% | 43% | 41% | 30% | \$33,633 | \$4,804 | \$5,704 |
| | 2010 | 40% | 41% | 42% | 37% | \$33,884 | \$5,140 | \$5,898 |
| | 2011 | 45% | 43% | 47% | 43% | \$24,728 | \$6,208 | \$6,184 |
| | 2012 | 39% | 41% | 46% | 48% | \$22,775 | \$4,923 | \$5,610 |
| | 2013 | 41% | 38% | 46% | 54% | \$21,924 | \$4,591 | \$5,409 |
| | 2014 | 39% | 35% | 46% | 59% | \$22,626 | \$4,911 | \$5,695 |
| | 2015 | 32% | 27% | 45% | 68% | \$19,798 | \$3,300 | \$5,318 |
| 2016 | 18% | 15% | 45% | 83% | \$18,576 | \$1,529 | \$5,017 | |
| Compliance Assessments | 2004 | 15% | 11% | 11% | 0% | \$4,084 | \$293 | \$295 |
| | 2005 | 17% | 11% | 10% | 1% | \$4,624 | \$308 | \$377 |
| | 2006 | 22% | 16% | 16% | 3% | \$4,916 | \$354 | \$462 |
| | 2007 | 19% | 17% | 15% | 17% | \$4,757 | \$391 | \$383 |
| | 2008 | 19% | 19% | 16% | 36% | \$7,661 | \$493 | \$698 |
| | 2009 | 16% | 17% | 14% | 50% | \$6,716 | \$494 | \$519 |
| | 2010 | 15% | 15% | 13% | 55% | \$7,259 | \$526 | \$568 |
| | 2011 | 14% | 14% | 12% | 62% | \$5,766 | \$421 | \$497 |
| | 2012 | 10% | 12% | 10% | 67% | \$5,258 | \$342 | \$377 |
| | 2013 | 10% | 12% | 10% | 74% | \$5,067 | \$290 | \$380 |
| | 2014 | 9% | 10% | 10% | 79% | \$4,911 | \$221 | \$319 |
| | 2015 | 7% | 7% | 9% | 86% | \$4,281 | \$119 | \$227 |
| 2016 | 3% | 3% | 9% | 94% | \$3,883 | \$53 | \$194 | |
| Write-off | 2004 | 2% | 2% | 2% | 0% | \$12,315 | \$101 | \$93 |
| | 2005 | 5% | 4% | 4% | 0% | \$13,193 | \$181 | \$167 |
| | 2006 | 7% | 5% | 5% | 0% | \$15,398 | \$344 | \$255 |
| | 2007 | 5% | 5% | 4% | 1% | \$15,352 | \$245 | \$248 |
| | 2008 | 5% | 6% | 4% | 6% | \$17,692 | \$284 | \$296 |
| | 2009 | 4% | 6% | 4% | 13% | \$18,931 | \$249 | \$312 |
| | 2010 | 4% | 5% | 4% | 22% | \$20,735 | \$282 | \$311 |
| | 2011 | 3% | 4% | 3% | 34% | \$33,831 | \$282 | \$346 |
| | 2012 | 3% | 3% | 3% | 46% | \$35,210 | \$262 | \$328 |
| | 2013 | 2% | 2% | 3% | 57% | \$35,433 | \$226 | \$312 |
| | 2014 | 2% | 2% | 2% | 69% | \$34,653 | \$170 | \$283 |
| | 2015 | 1% | 1% | 2% | 81% | \$35,107 | \$122 | \$268 |
| 2016 | 0% | 1% | 2% | 94% | \$34,220 | \$31 | \$247 | |
| All | 2004 | 29% | 28% | 28% | 1% | \$50,349 | \$6,880 | \$6,975 |
| | 2005 | 30% | 28% | 27% | 1% | \$50,457 | \$6,984 | \$6,521 |
| | 2006 | 29% | 27% | 26% | 2% | \$52,154 | \$7,009 | \$6,729 |
| | 2007 | 26% | 28% | 26% | 7% | \$52,125 | \$6,312 | \$6,402 |
| | 2008 | 25% | 28% | 25% | 16% | \$59,231 | \$5,980 | \$7,256 |
| | 2009 | 24% | 26% | 24% | 25% | \$59,280 | \$5,548 | \$6,535 |
| | 2010 | 24% | 24% | 24% | 34% | \$61,878 | \$5,948 | \$6,777 |
| | 2011 | 23% | 23% | 24% | 41% | \$64,326 | \$6,911 | \$7,026 |
| | 2012 | 20% | 20% | 23% | 49% | \$63,244 | \$5,527 | \$6,315 |
| | 2013 | 20% | 18% | 22% | 57% | \$62,424 | \$5,107 | \$6,101 |
| | 2014 | 18% | 17% | 22% | 66% | \$62,190 | \$5,302 | \$6,298 |
| | 2015 | 15% | 13% | 21% | 76% | \$59,185 | \$3,541 | \$5,813 |
| 2016 | 8% | 7% | 21% | 90% | \$56,679 | \$1,613 | \$5,458 | |

TABLE A2. Form 1040 Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 70% | 66% | 66% | 2% | \$63,434 | \$26,527 | \$25,267 |
| | 2005 | 72% | 68% | 68% | 5% | \$62,073 | \$27,220 | \$24,770 |
| | 2006 | 71% | 70% | 68% | 9% | \$64,730 | \$27,874 | \$25,918 |
| | 2007 | 71% | 71% | 70% | 14% | \$71,421 | \$30,446 | \$29,576 |
| | 2008 | 70% | 72% | 70% | 18% | \$75,256 | \$31,470 | \$32,800 |
| | 2009 | 65% | 70% | 69% | 25% | \$80,944 | \$32,655 | \$36,516 |
| | 2010 | 65% | 68% | 70% | 29% | \$89,183 | \$36,590 | \$41,989 |
| | 2011 | 63% | 65% | 70% | 35% | \$99,170 | \$38,376 | \$45,388 |
| | 2012 | 60% | 60% | 70% | 41% | \$106,428 | \$39,527 | \$48,964 |
| | 2013 | 55% | 53% | 69% | 50% | \$113,063 | \$37,859 | \$51,022 |
| | 2014 | 49% | 46% | 69% | 62% | \$116,404 | \$33,251 | \$52,154 |
| | 2015 | 39% | 35% | 68% | 71% | \$123,411 | \$26,737 | \$55,925 |
| 2016 | 24% | 20% | 68% | 62% | \$130,613 | \$14,229 | \$59,345 | |
| Compliance Assessments | 2004 | 50% | 48% | 48% | 1% | \$16,156 | \$2,954 | \$3,272 |
| | 2005 | 56% | 55% | 54% | 11% | \$20,139 | \$3,841 | \$4,814 |
| | 2006 | 55% | 57% | 54% | 23% | \$28,880 | \$4,710 | \$6,070 |
| | 2007 | 53% | 57% | 54% | 32% | \$41,646 | \$6,066 | \$8,438 |
| | 2008 | 49% | 53% | 51% | 40% | \$44,639 | \$7,284 | \$9,838 |
| | 2009 | 46% | 50% | 51% | 47% | \$47,950 | \$7,321 | \$10,686 |
| | 2010 | 46% | 47% | 52% | 49% | \$53,619 | \$7,119 | \$11,053 |
| | 2011 | 42% | 41% | 49% | 56% | \$77,558 | \$8,093 | \$13,594 |
| | 2012 | 39% | 37% | 49% | 62% | \$80,045 | \$7,400 | \$13,927 |
| | 2013 | 35% | 33% | 49% | 68% | \$69,407 | \$5,970 | \$12,615 |
| | 2014 | 34% | 30% | 50% | 74% | \$66,122 | \$5,307 | \$12,033 |
| | 2015 | 28% | 24% | 49% | 78% | \$56,184 | \$3,452 | \$10,868 |
| 2016 | 20% | 16% | 50% | 62% | \$55,522 | \$2,022 | \$11,067 | |
| Write-off | 2004 | 18% | 16% | 16% | 0% | \$36,299 | \$1,690 | \$1,612 |
| | 2005 | 19% | 17% | 16% | 1% | \$38,059 | \$1,959 | \$1,796 |
| | 2006 | 20% | 18% | 17% | 4% | \$33,439 | \$1,901 | \$1,805 |
| | 2007 | 20% | 19% | 17% | 12% | \$35,996 | \$2,054 | \$2,006 |
| | 2008 | 20% | 19% | 17% | 22% | \$44,584 | \$2,277 | \$2,363 |
| | 2009 | 16% | 18% | 16% | 35% | \$46,433 | \$2,121 | \$2,429 |
| | 2010 | 17% | 18% | 16% | 51% | \$59,527 | \$3,134 | \$3,489 |
| | 2011 | 16% | 17% | 17% | 55% | \$46,288 | \$1,753 | \$2,139 |
| | 2012 | 14% | 15% | 16% | 69% | \$54,205 | \$1,681 | \$2,286 |
| | 2013 | 11% | 12% | 16% | 82% | \$70,989 | \$1,547 | \$2,755 |
| | 2014 | 8% | 9% | 15% | 94% | \$76,506 | \$1,182 | \$2,853 |
| | 2015 | 6% | 6% | 15% | 96% | \$83,644 | \$712 | \$2,801 |
| 2016 | 3% | 4% | 15% | 98% | \$82,995 | \$336 | \$2,777 | |
| All | 2004 | 56% | 53% | 53% | 1% | \$115,888 | \$31,171 | \$30,150 |
| | 2005 | 58% | 56% | 55% | 5% | \$120,270 | \$33,020 | \$31,380 |
| | 2006 | 59% | 58% | 57% | 10% | \$127,049 | \$34,486 | \$33,793 |
| | 2007 | 59% | 60% | 58% | 16% | \$149,062 | \$38,565 | \$40,020 |
| | 2008 | 58% | 59% | 58% | 23% | \$164,478 | \$41,031 | \$45,001 |
| | 2009 | 53% | 57% | 57% | 31% | \$175,327 | \$42,097 | \$49,631 |
| | 2010 | 53% | 55% | 57% | 37% | \$202,329 | \$46,843 | \$56,531 |
| | 2011 | 51% | 53% | 58% | 42% | \$223,016 | \$48,223 | \$61,122 |
| | 2012 | 49% | 48% | 58% | 50% | \$240,678 | \$48,608 | \$65,177 |
| | 2013 | 44% | 43% | 56% | 59% | \$253,459 | \$45,376 | \$66,392 |
| | 2014 | 39% | 37% | 55% | 70% | \$259,033 | \$39,740 | \$67,040 |
| | 2015 | 31% | 28% | 55% | 77% | \$263,239 | \$30,901 | \$69,595 |
| 2016 | 19% | 16% | 55% | 68% | \$269,129 | \$16,586 | \$73,189 | |

TABLE A3. Form 940 Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 31% | 31% | 31% | 1% | \$609 | \$123 | \$117 |
| | 2005 | 34% | 33% | 32% | 1% | \$907 | \$125 | \$170 |
| | 2006 | 38% | 35% | 34% | 3% | \$613 | \$116 | \$118 |
| | 2007 | 34% | 37% | 34% | 8% | \$802 | \$113 | \$149 |
| | 2008 | 34% | 39% | 36% | 21% | \$755 | \$108 | \$128 |
| | 2009 | 32% | 35% | 35% | 33% | \$754 | \$85 | \$118 |
| | 2010 | 33% | 33% | 36% | 42% | \$695 | \$85 | \$105 |
| | 2011 | 33% | 31% | 36% | 49% | \$559 | \$87 | \$107 |
| | 2012 | 29% | 29% | 35% | 57% | \$581 | \$78 | \$113 |
| | 2013 | 29% | 27% | 36% | 64% | \$551 | \$78 | \$105 |
| | 2014 | 26% | 24% | 35% | 72% | \$566 | \$79 | \$111 |
| 2015 | 20% | 18% | 35% | 78% | \$505 | \$71 | \$115 | |
| 2016 | 9% | 8% | 35% | 91% | \$507 | \$29 | \$114 | |
| Compliance Assessments | 2004 | 17% | 13% | 13% | 1% | \$948 | \$80 | \$83 |
| | 2005 | 19% | 14% | 14% | 1% | \$864 | \$90 | \$77 |
| | 2006 | 20% | 16% | 15% | 2% | \$880 | \$78 | \$82 |
| | 2007 | 17% | 16% | 14% | 11% | \$973 | \$74 | \$89 |
| | 2008 | 18% | 20% | 16% | 28% | \$1,003 | \$79 | \$99 |
| | 2009 | 15% | 17% | 14% | 45% | \$1,050 | \$61 | \$106 |
| | 2010 | 16% | 16% | 13% | 57% | \$822 | \$73 | \$70 |
| | 2011 | 13% | 14% | 12% | 65% | \$817 | \$60 | \$67 |
| | 2012 | 10% | 13% | 11% | 72% | \$902 | \$44 | \$84 |
| | 2013 | 8% | 9% | 8% | 81% | \$689 | \$50 | \$44 |
| | 2014 | 7% | 9% | 8% | 85% | \$692 | \$31 | \$49 |
| 2015 | 7% | 8% | 10% | 88% | \$628 | \$26 | \$55 | |
| 2016 | 3% | 3% | 9% | 96% | \$649 | \$8 | \$49 | |
| Write-off | 2004 | 1% | 1% | 1% | 0% | \$2,151 | \$9 | \$11 |
| | 2005 | 3% | 2% | 2% | 0% | \$1,907 | \$12 | \$13 |
| | 2006 | 4% | 3% | 2% | 0% | \$1,970 | \$16 | \$15 |
| | 2007 | 3% | 3% | 2% | 1% | \$1,832 | \$19 | \$15 |
| | 2008 | 3% | 3% | 2% | 5% | \$2,101 | \$24 | \$16 |
| | 2009 | 2% | 3% | 2% | 12% | \$2,214 | \$21 | \$17 |
| | 2010 | 2% | 3% | 2% | 20% | \$2,319 | \$17 | \$17 |
| | 2011 | 2% | 2% | 2% | 30% | \$2,489 | \$12 | \$16 |
| | 2012 | 2% | 2% | 2% | 40% | \$2,454 | \$12 | \$15 |
| | 2013 | 2% | 2% | 2% | 51% | \$2,436 | \$10 | \$14 |
| | 2014 | 1% | 1% | 2% | 62% | \$2,425 | \$8 | \$12 |
| 2015 | 1% | 1% | 2% | 77% | \$2,436 | \$4 | \$12 | |
| 2016 | 0% | 0% | 2% | 91% | \$2,379 | \$1 | \$11 | |
| All | 2004 | 18% | 17% | 17% | 0% | \$3,708 | \$213 | \$212 |
| | 2005 | 19% | 17% | 17% | 1% | \$3,677 | \$227 | \$260 |
| | 2006 | 20% | 18% | 18% | 2% | \$3,462 | \$210 | \$216 |
| | 2007 | 19% | 20% | 18% | 6% | \$3,607 | \$206 | \$252 |
| | 2008 | 18% | 20% | 18% | 15% | \$3,859 | \$210 | \$242 |
| | 2009 | 16% | 18% | 17% | 25% | \$4,018 | \$167 | \$241 |
| | 2010 | 17% | 17% | 17% | 35% | \$3,836 | \$176 | \$191 |
| | 2011 | 16% | 16% | 17% | 43% | \$3,865 | \$159 | \$190 |
| | 2012 | 14% | 14% | 17% | 52% | \$3,937 | \$133 | \$211 |
| | 2013 | 14% | 13% | 17% | 60% | \$3,677 | \$138 | \$163 |
| | 2014 | 12% | 11% | 16% | 69% | \$3,682 | \$118 | \$171 |
| 2015 | 9% | 8% | 16% | 79% | \$3,569 | \$101 | \$182 | |
| 2016 | 4% | 3% | 15% | 91% | \$3,535 | \$38 | \$174 | |

TABLE A4. Form 1065 Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 18% | 18% | 18% | 1% | \$133 | \$14 | \$15 |
| | 2005 | 20% | 18% | 18% | 0% | \$101 | \$12 | \$11 |
| | 2006 | 34% | 30% | 30% | 0% | \$111 | \$24 | \$22 |
| | 2007 | 29% | 30% | 29% | 11% | \$138 | \$26 | \$27 |
| | 2008 | 29% | 31% | 30% | 24% | \$144 | \$29 | \$30 |
| | 2009 | 23% | 27% | 28% | 34% | \$220 | \$33 | \$43 |
| | 2010 | 24% | 28% | 27% | 41% | \$282 | \$50 | \$60 |
| | 2011 | 24% | 22% | 26% | 49% | \$321 | \$59 | \$67 |
| | 2012 | 18% | 18% | 23% | 56% | \$465 | \$90 | \$86 |
| | 2013 | 18% | 15% | 21% | 64% | \$549 | \$72 | \$95 |
| | 2014 | 15% | 13% | 20% | 67% | \$612 | \$68 | \$101 |
| | 2015 | 12% | 10% | 19% | 73% | \$680 | \$61 | \$102 |
| 2016 | 6% | 6% | 19% | 85% | \$726 | \$33 | \$105 | |
| Compliance Assessments | 2004 | 19% | 19% | 19% | 27% | \$1 | \$0 | \$0 |
| | 2005 | 28% | 29% | 29% | 3% | \$1 | \$0 | \$0 |
| | 2006 | 30% | 25% | 25% | 4% | \$105 | \$1 | \$2 |
| | 2007 | 36% | 25% | 22% | 4% | \$10 | \$1 | \$1 |
| | 2008 | 22% | 28% | 26% | 13% | \$1 | \$1 | \$1 |
| | 2009 | 12% | 21% | 19% | 25% | \$2 | \$1 | \$1 |
| | 2010 | 41% | 38% | 35% | 32% | \$27 | \$27 | \$7 |
| | 2011 | 16% | 15% | 25% | 57% | \$130 | \$0 | \$3 |
| | 2012 | 30% | 42% | 36% | 36% | \$134 | \$0 | \$2 |
| | 2013 | 30% | 39% | 29% | 30% | \$0 | \$0 | \$0 |
| | 2014 | 8% | 21% | 25% | 54% | \$12 | \$2 | \$1 |
| | 2015 | 23% | 19% | 26% | 67% | \$3 | \$3 | \$0 |
| 2016 | 50% | 37% | 30% | 50% | \$46 | \$14 | \$6 | |
| Write-off | 2004 | 3% | 2% | 2% | 1% | \$44 | \$1 | \$0 |
| | 2005 | 5% | 3% | 3% | 1% | \$61 | \$1 | \$1 |
| | 2006 | 5% | 4% | 4% | 1% | \$82 | \$2 | \$1 |
| | 2007 | 4% | 5% | 4% | 4% | \$78 | \$1 | \$1 |
| | 2008 | 4% | 5% | 4% | 11% | \$73 | \$2 | \$2 |
| | 2009 | 4% | 5% | 5% | 24% | \$69 | \$2 | \$2 |
| | 2010 | 4% | 6% | 5% | 37% | \$74 | \$2 | \$2 |
| | 2011 | 4% | 4% | 5% | 52% | \$103 | \$2 | \$3 |
| | 2012 | 3% | 3% | 4% | 65% | \$141 | \$3 | \$4 |
| | 2013 | 3% | 2% | 4% | 73% | \$197 | \$4 | \$5 |
| | 2014 | 2% | 1% | 3% | 81% | \$282 | \$3 | \$7 |
| | 2015 | 1% | 1% | 3% | 87% | \$398 | \$2 | \$9 |
| 2016 | 0% | 0% | 2% | 98% | \$483 | \$1 | \$10 | |
| All | 2004 | 15% | 15% | 15% | 1% | \$177 | \$15 | \$15 |
| | 2005 | 15% | 13% | 13% | 1% | \$163 | \$14 | \$12 |
| | 2006 | 24% | 21% | 21% | 1% | \$298 | \$27 | \$25 |
| | 2007 | 23% | 24% | 23% | 9% | \$225 | \$28 | \$29 |
| | 2008 | 22% | 24% | 23% | 20% | \$218 | \$32 | \$32 |
| | 2009 | 18% | 21% | 22% | 32% | \$291 | \$36 | \$46 |
| | 2010 | 19% | 23% | 22% | 40% | \$383 | \$79 | \$68 |
| | 2011 | 19% | 17% | 20% | 50% | \$554 | \$62 | \$74 |
| | 2012 | 13% | 13% | 17% | 59% | \$740 | \$93 | \$92 |
| | 2013 | 12% | 10% | 15% | 67% | \$746 | \$76 | \$101 |
| | 2014 | 9% | 8% | 13% | 73% | \$906 | \$73 | \$109 |
| | 2015 | 7% | 5% | 11% | 80% | \$1,081 | \$66 | \$111 |
| 2016 | 3% | 3% | 11% | 91% | \$1,255 | \$48 | \$121 | |

TABLE A5. Form 1120 Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 40% | 40% | 40% | 1% | \$1,232 | \$431 | \$372 |
| | 2005 | 43% | 41% | 41% | 1% | \$703 | \$190 | \$161 |
| | 2006 | 47% | 44% | 44% | 1% | \$1,474 | \$634 | \$463 |
| | 2007 | 46% | 47% | 45% | 7% | \$3,259 | \$1,694 | \$1,086 |
| | 2008 | 49% | 50% | 49% | 16% | \$986 | \$464 | \$346 |
| | 2009 | 46% | 47% | 48% | 26% | \$1,716 | \$924 | \$728 |
| | 2010 | 48% | 54% | 52% | 31% | \$1,685 | \$642 | \$616 |
| | 2011 | 44% | 42% | 49% | 41% | \$1,822 | \$403 | \$625 |
| | 2012 | 33% | 36% | 46% | 51% | \$1,807 | \$210 | \$500 |
| | 2013 | 32% | 30% | 43% | 60% | \$2,922 | \$227 | \$460 |
| | 2014 | 27% | 25% | 41% | 66% | \$1,841 | \$435 | \$484 |
| 2015 | 22% | 19% | 39% | 73% | \$1,998 | \$512 | \$486 | |
| 2016 | 12% | 11% | 38% | 86% | \$1,520 | \$145 | \$487 | |
| Compliance Assessments | 2004 | 12% | 14% | 14% | 7% | \$1,752 | \$136 | \$29 |
| | 2005 | 17% | 16% | 15% | 7% | \$1,675 | \$10 | \$9 |
| | 2006 | 25% | 17% | 16% | 10% | \$1,947 | \$2 | \$35 |
| | 2007 | 23% | 20% | 17% | 17% | \$2,323 | \$4 | \$70 |
| | 2008 | 20% | 23% | 18% | 36% | \$3,440 | \$14 | \$139 |
| | 2009 | 25% | 23% | 18% | 39% | \$2,620 | \$88 | \$47 |
| | 2010 | 20% | 23% | 19% | 54% | \$3,047 | \$13 | \$38 |
| | 2011 | 13% | 14% | 17% | 69% | \$3,891 | \$152 | \$113 |
| | 2012 | 11% | 15% | 17% | 70% | \$3,865 | \$27 | \$99 |
| | 2013 | 14% | 12% | 16% | 76% | \$3,324 | \$3 | \$52 |
| | 2014 | 14% | 14% | 17% | 75% | \$3,186 | \$9 | \$37 |
| 2015 | 9% | 11% | 17% | 84% | \$3,193 | \$1 | \$16 | |
| 2016 | 4% | 5% | 14% | 92% | \$3,438 | \$2 | \$27 | |
| Write-off | 2004 | 1% | 1% | 1% | 1% | \$13,533 | \$253 | \$15 |
| | 2005 | 3% | 3% | 3% | 2% | \$9,447 | \$259 | \$11 |
| | 2006 | 3% | 3% | 3% | 1% | \$9,552 | \$279 | \$10 |
| | 2007 | 3% | 3% | 3% | 2% | \$9,308 | \$26 | \$11 |
| | 2008 | 2% | 3% | 3% | 5% | \$9,312 | \$4 | \$14 |
| | 2009 | 2% | 3% | 3% | 10% | \$9,629 | \$5 | \$12 |
| | 2010 | 3% | 5% | 3% | 20% | \$10,128 | \$6 | \$13 |
| | 2011 | 3% | 4% | 4% | 36% | \$10,602 | \$8 | \$11 |
| | 2012 | 3% | 3% | 4% | 56% | \$11,098 | \$18 | \$13 |
| | 2013 | 3% | 2% | 4% | 72% | \$11,853 | \$3 | \$14 |
| | 2014 | 2% | 1% | 4% | 85% | \$2,987 | \$3 | \$18 |
| 2015 | 1% | 1% | 4% | 93% | \$3,200 | \$2 | \$15 | |
| 2016 | 1% | 0% | 3% | 98% | \$3,897 | \$1 | \$23 | |
| All | 2004 | 32% | 32% | 31% | 1% | \$16,517 | \$820 | \$415 |
| | 2005 | 32% | 30% | 30% | 1% | \$11,824 | \$460 | \$181 |
| | 2006 | 31% | 29% | 28% | 1% | \$12,974 | \$915 | \$507 |
| | 2007 | 32% | 32% | 31% | 5% | \$14,890 | \$1,724 | \$1,166 |
| | 2008 | 32% | 33% | 32% | 12% | \$13,738 | \$481 | \$499 |
| | 2009 | 30% | 31% | 32% | 20% | \$13,965 | \$1,017 | \$787 |
| | 2010 | 37% | 42% | 40% | 29% | \$14,860 | \$660 | \$667 |
| | 2011 | 35% | 34% | 39% | 40% | \$16,315 | \$563 | \$750 |
| | 2012 | 26% | 28% | 37% | 52% | \$16,770 | \$256 | \$611 |
| | 2013 | 24% | 23% | 33% | 63% | \$18,099 | \$233 | \$526 |
| | 2014 | 20% | 18% | 30% | 71% | \$8,014 | \$447 | \$538 |
| 2015 | 15% | 13% | 27% | 80% | \$8,391 | \$515 | \$517 | |
| 2016 | 8% | 7% | 25% | 90% | \$8,856 | \$147 | \$536 | |

TABLE A6. TFRP Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 61% | 49% | 49% | 5% | \$59 | \$15 | \$22 |
| | 2005 | 59% | 46% | 47% | 10% | \$54 | \$15 | \$18 |
| | 2006 | 56% | 43% | 45% | 16% | \$49 | \$14 | \$19 |
| | 2007 | 34% | 42% | 46% | 41% | \$2,806 | \$455 | \$1,185 |
| | 2008 | 30% | 36% | 42% | 45% | \$4,649 | \$636 | \$1,646 |
| | 2009 | 27% | 31% | 40% | 52% | \$6,383 | \$738 | \$2,050 |
| | 2010 | 26% | 28% | 40% | 58% | \$6,776 | \$791 | \$2,271 |
| | 2011 | 25% | 25% | 40% | 66% | \$7,799 | \$861 | \$2,644 |
| | 2012 | 24% | 23% | 41% | 70% | \$8,590 | \$927 | \$2,889 |
| | 2013 | 22% | 19% | 41% | 77% | \$9,333 | \$910 | \$3,116 |
| | 2014 | 18% | 14% | 39% | 88% | \$9,698 | \$740 | \$2,940 |
| 2015 | 14% | 10% | 37% | 91% | \$9,692 | \$560 | \$2,850 | |
| 2016 | 8% | 6% | 36% | 87% | \$9,403 | \$287 | \$2,691 | |
| Compliance Assessments | 2004 | 28% | 32% | 33% | 9% | \$12,598 | \$1,411 | \$2,729 |
| | 2005 | 28% | 31% | 33% | 20% | \$12,609 | \$1,471 | \$2,814 |
| | 2006 | 28% | 30% | 32% | 28% | \$12,617 | \$1,458 | \$2,847 |
| | 2007 | 23% | 25% | 28% | 30% | \$9,872 | \$883 | \$1,874 |
| | 2008 | 22% | 24% | 29% | 41% | \$7,592 | \$583 | \$1,477 |
| | 2009 | 21% | 22% | 31% | 51% | \$5,988 | \$504 | \$1,354 |
| | 2010 | 22% | 20% | 32% | 56% | \$5,530 | \$455 | \$1,267 |
| | 2011 | 21% | 18% | 33% | 62% | \$5,484 | \$480 | \$1,436 |
| | 2012 | 19% | 16% | 33% | 69% | \$5,906 | \$485 | \$1,570 |
| | 2013 | 16% | 12% | 32% | 80% | \$5,400 | \$380 | \$1,412 |
| | 2014 | 14% | 9% | 32% | 91% | \$4,949 | \$305 | \$1,314 |
| 2015 | 10% | 6% | 30% | 94% | \$4,539 | \$178 | \$1,147 | |
| 2016 | 5% | 3% | 30% | 66% | \$4,321 | \$74 | \$1,131 | |
| Write-off | 2004 | 22% | 19% | 19% | 2% | \$47 | \$2 | \$4 |
| | 2005 | 28% | 19% | 20% | 5% | \$39 | \$2 | \$6 |
| | 2006 | 24% | 17% | 18% | 9% | \$38 | \$2 | \$6 |
| | 2007 | 19% | 18% | 21% | 42% | \$398 | \$35 | \$88 |
| | 2008 | 15% | 14% | 17% | 45% | \$1,296 | \$58 | \$164 |
| | 2009 | 10% | 11% | 15% | 51% | \$1,858 | \$56 | \$187 |
| | 2010 | 9% | 9% | 15% | 57% | \$2,617 | \$70 | \$279 |
| | 2011 | 7% | 8% | 12% | 53% | \$3,132 | \$56 | \$260 |
| | 2012 | 6% | 6% | 11% | 66% | \$3,309 | \$55 | \$269 |
| | 2013 | 5% | 5% | 11% | 82% | \$3,797 | \$56 | \$322 |
| | 2014 | 4% | 4% | 11% | 98% | \$3,687 | \$46 | \$294 |
| 2015 | 3% | 3% | 10% | 98% | \$3,661 | \$26 | \$299 | |
| 2016 | 1% | 2% | 10% | 99% | \$3,984 | \$12 | \$324 | |
| All | 2004 | 30% | 33% | 34% | 9% | \$12,705 | \$1,428 | \$2,755 |
| | 2005 | 30% | 32% | 33% | 19% | \$12,702 | \$1,489 | \$2,839 |
| | 2006 | 29% | 30% | 33% | 27% | \$12,704 | \$1,474 | \$2,871 |
| | 2007 | 27% | 31% | 34% | 35% | \$13,077 | \$1,373 | \$3,147 |
| | 2008 | 25% | 29% | 34% | 43% | \$13,536 | \$1,277 | \$3,288 |
| | 2009 | 23% | 26% | 34% | 51% | \$14,230 | \$1,298 | \$3,591 |
| | 2010 | 22% | 23% | 33% | 57% | \$14,924 | \$1,317 | \$3,816 |
| | 2011 | 21% | 20% | 34% | 63% | \$16,416 | \$1,396 | \$4,340 |
| | 2012 | 20% | 18% | 34% | 69% | \$17,805 | \$1,468 | \$4,728 |
| | 2013 | 17% | 15% | 33% | 78% | \$18,530 | \$1,347 | \$4,851 |
| | 2014 | 14% | 11% | 32% | 90% | \$18,335 | \$1,091 | \$4,548 |
| 2015 | 11% | 8% | 31% | 93% | \$17,891 | \$764 | \$4,296 | |
| 2016 | 6% | 4% | 29% | 84% | \$17,709 | \$373 | \$4,145 | |

TABLE A7. Other Individual Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 31% | 37% | 47% | 0% | \$440 | \$39 | \$197 |
| | 2005 | 49% | 49% | 49% | 2% | \$547 | \$58 | \$322 |
| | 2006 | 48% | 48% | 47% | 9% | \$1,328 | \$288 | \$627 |
| | 2007 | 51% | 51% | 47% | 15% | \$2,455 | \$648 | \$1,046 |
| | 2008 | 49% | 48% | 47% | 22% | \$1,919 | \$365 | \$789 |
| | 2009 | 48% | 48% | 48% | 27% | \$2,125 | \$409 | \$883 |
| | 2010 | 47% | 48% | 48% | 35% | \$2,554 | \$435 | \$1,097 |
| | 2011 | 47% | 48% | 47% | 44% | \$2,683 | \$472 | \$1,250 |
| | 2012 | 46% | 46% | 46% | 50% | \$2,982 | \$544 | \$1,321 |
| | 2013 | 44% | 44% | 47% | 59% | \$3,534 | \$572 | \$1,672 |
| | 2014 | 40% | 40% | 46% | 73% | \$4,948 | \$1,005 | \$2,242 |
| 2015 | 32% | 39% | 47% | 80% | \$5,881 | \$968 | \$2,730 | |
| 2016 | 23% | 57% | 49% | 25% | \$5,413 | \$235 | \$2,560 | |
| Compliance Assessments | 2004 | 39% | 32% | 53% | 4% | \$67 | \$4 | \$44 |
| | 2005 | 29% | 22% | 49% | 3% | \$186 | \$6 | \$79 |
| | 2006 | 39% | 37% | 53% | 12% | \$406 | \$40 | \$239 |
| | 2007 | 39% | 42% | 48% | 18% | \$408 | \$41 | \$228 |
| | 2008 | 49% | 45% | 48% | 17% | \$197 | \$33 | \$123 |
| | 2009 | 43% | 45% | 45% | 28% | \$253 | \$26 | \$146 |
| | 2010 | 49% | 44% | 44% | 39% | \$246 | \$29 | \$120 |
| | 2011 | 44% | 44% | 45% | 54% | \$314 | \$31 | \$126 |
| | 2012 | 35% | 41% | 43% | 60% | \$447 | \$23 | \$220 |
| | 2013 | 42% | 39% | 44% | 66% | \$432 | \$122 | \$125 |
| | 2014 | 34% | 38% | 51% | 75% | \$214 | \$25 | \$125 |
| 2015 | 27% | 34% | 48% | 82% | \$249 | \$24 | \$116 | |
| 2016 | 13% | 35% | 46% | 62% | \$297 | \$15 | \$110 | |
| Write-off | 2004 | 15% | 11% | 49% | 3% | \$259 | \$14 | \$121 |
| | 2005 | 13% | 12% | 50% | 3% | \$443 | \$12 | \$191 |
| | 2006 | 16% | 15% | 49% | 6% | \$729 | \$18 | \$435 |
| | 2007 | 15% | 15% | 49% | 6% | \$767 | \$12 | \$455 |
| | 2008 | 15% | 15% | 48% | 12% | \$976 | \$22 | \$483 |
| | 2009 | 13% | 13% | 50% | 18% | \$754 | \$25 | \$366 |
| | 2010 | 12% | 13% | 48% | 23% | \$807 | \$21 | \$400 |
| | 2011 | 12% | 12% | 48% | 29% | \$769 | \$18 | \$384 |
| | 2012 | 11% | 12% | 46% | 45% | \$763 | \$16 | \$335 |
| | 2013 | 11% | 12% | 48% | 72% | \$1,005 | \$24 | \$470 |
| | 2014 | 8% | 9% | 46% | 95% | \$1,165 | \$20 | \$564 |
| 2015 | 5% | 10% | 47% | 97% | \$1,249 | \$11 | \$552 | |
| 2016 | 3% | 10% | 46% | 96% | \$1,566 | \$5 | \$640 | |
| All | 2004 | 25% | 26% | 48% | 1% | \$765 | \$57 | \$362 |
| | 2005 | 35% | 34% | 49% | 2% | \$1,176 | \$76 | \$591 |
| | 2006 | 40% | 39% | 48% | 8% | \$2,463 | \$347 | \$1,300 |
| | 2007 | 44% | 44% | 48% | 13% | \$3,631 | \$701 | \$1,730 |
| | 2008 | 40% | 39% | 48% | 19% | \$3,092 | \$420 | \$1,396 |
| | 2009 | 39% | 39% | 48% | 25% | \$3,132 | \$459 | \$1,394 |
| | 2010 | 40% | 40% | 48% | 33% | \$3,607 | \$485 | \$1,616 |
| | 2011 | 40% | 40% | 47% | 41% | \$3,766 | \$521 | \$1,759 |
| | 2012 | 39% | 40% | 46% | 50% | \$4,193 | \$582 | \$1,875 |
| | 2013 | 37% | 37% | 47% | 62% | \$4,971 | \$718 | \$2,267 |
| | 2014 | 34% | 34% | 46% | 77% | \$6,328 | \$1,050 | \$2,931 |
| 2015 | 26% | 33% | 47% | 83% | \$7,379 | \$1,004 | \$3,398 | |
| 2016 | 21% | 52% | 49% | 32% | \$7,277 | \$254 | \$3,313 | |

TABLE A8. Other Business Recovery Model Results (\$ in Millions)

| Financial Class | Year | Actual Recovery | Predicted Recovery with Truncation | Predicted Recovery | Percent Truncated | Total Balance | Observed Value | Estimated Value |
|------------------------|------|-----------------|------------------------------------|--------------------|-------------------|---------------|----------------|-----------------|
| Taxes Receivable | 2004 | 48% | 47% | 47% | 1% | \$7,492 | \$4,862 | \$2,338 |
| | 2005 | 50% | 47% | 47% | 1% | \$7,037 | \$4,456 | \$2,114 |
| | 2006 | 44% | 43% | 42% | 1% | \$7,140 | \$4,612 | \$1,940 |
| | 2007 | 41% | 42% | 42% | 5% | \$8,458 | \$5,401 | \$2,353 |
| | 2008 | 41% | 43% | 43% | 12% | \$8,618 | \$5,544 | \$2,587 |
| | 2009 | 39% | 42% | 43% | 20% | \$9,488 | \$6,110 | \$2,908 |
| | 2010 | 38% | 39% | 43% | 27% | \$10,800 | \$6,942 | \$3,212 |
| | 2011 | 38% | 36% | 43% | 35% | \$9,810 | \$5,500 | \$2,780 |
| | 2012 | 33% | 35% | 43% | 40% | \$10,085 | \$5,088 | \$2,496 |
| | 2013 | 34% | 32% | 43% | 49% | \$8,754 | \$3,823 | \$2,209 |
| | 2014 | 31% | 32% | 44% | 53% | \$8,785 | \$2,908 | \$2,260 |
| | 2015 | 28% | 26% | 44% | 61% | \$8,355 | \$2,061 | \$2,079 |
| 2016 | 19% | 16% | 45% | 77% | \$8,426 | \$1,394 | \$2,165 | |
| Compliance Assessments | 2004 | 19% | 19% | 18% | 0% | \$8,690 | \$161 | \$587 |
| | 2005 | 20% | 19% | 18% | 0% | \$8,927 | \$239 | \$813 |
| | 2006 | 21% | 20% | 19% | 1% | \$4,179 | \$202 | \$568 |
| | 2007 | 19% | 21% | 19% | 12% | \$2,940 | \$191 | \$397 |
| | 2008 | 19% | 21% | 20% | 23% | \$4,107 | \$179 | \$429 |
| | 2009 | 19% | 19% | 21% | 36% | \$2,715 | \$211 | \$415 |
| | 2010 | 18% | 17% | 20% | 45% | \$2,454 | \$207 | \$380 |
| | 2011 | 15% | 15% | 20% | 54% | \$2,471 | \$219 | \$366 |
| | 2012 | 13% | 13% | 21% | 64% | \$2,372 | \$159 | \$389 |
| | 2013 | 12% | 11% | 20% | 75% | \$2,802 | \$143 | \$439 |
| | 2014 | 11% | 10% | 20% | 78% | \$2,318 | \$136 | \$346 |
| | 2015 | 9% | 6% | 19% | 85% | \$2,262 | \$132 | \$323 |
| 2016 | 5% | 3% | 19% | 94% | \$1,938 | \$59 | \$301 | |
| Write-off | 2004 | 3% | 3% | 3% | 1% | \$2,894 | \$53 | \$34 |
| | 2005 | 6% | 5% | 5% | 1% | \$3,500 | \$65 | \$52 |
| | 2006 | 9% | 6% | 6% | 1% | \$10,150 | \$79 | \$75 |
| | 2007 | 5% | 6% | 5% | 2% | \$10,647 | \$48 | \$73 |
| | 2008 | 5% | 6% | 5% | 5% | \$11,853 | \$66 | \$80 |
| | 2009 | 4% | 5% | 5% | 10% | \$12,624 | \$42 | \$83 |
| | 2010 | 5% | 6% | 6% | 18% | \$13,029 | \$49 | \$98 |
| | 2011 | 5% | 5% | 6% | 28% | \$13,634 | \$47 | \$113 |
| | 2012 | 4% | 5% | 6% | 39% | \$13,853 | \$38 | \$112 |
| | 2013 | 4% | 4% | 6% | 50% | \$5,680 | \$45 | \$115 |
| | 2014 | 3% | 3% | 6% | 66% | \$4,427 | \$36 | \$112 |
| | 2015 | 2% | 2% | 6% | 82% | \$4,304 | \$28 | \$109 |
| 2016 | 1% | 1% | 6% | 96% | \$4,424 | \$23 | \$111 | |
| All | 2004 | 33% | 32% | 32% | 1% | \$19,077 | \$5,075 | \$2,958 |
| | 2005 | 33% | 31% | 31% | 1% | \$19,463 | \$4,760 | \$2,979 |
| | 2006 | 28% | 26% | 26% | 1% | \$21,468 | \$4,893 | \$2,583 |
| | 2007 | 26% | 28% | 27% | 6% | \$22,045 | \$5,641 | \$2,823 |
| | 2008 | 25% | 26% | 26% | 13% | \$24,578 | \$5,790 | \$3,096 |
| | 2009 | 24% | 25% | 26% | 21% | \$24,828 | \$6,363 | \$3,406 |
| | 2010 | 23% | 23% | 26% | 29% | \$26,283 | \$7,199 | \$3,690 |
| | 2011 | 21% | 21% | 25% | 37% | \$25,915 | \$5,766 | \$3,259 |
| | 2012 | 18% | 19% | 25% | 46% | \$26,311 | \$5,286 | \$2,997 |
| | 2013 | 18% | 17% | 24% | 56% | \$17,237 | \$4,011 | \$2,763 |
| | 2014 | 16% | 16% | 25% | 64% | \$15,530 | \$3,080 | \$2,718 |
| | 2015 | 14% | 13% | 25% | 74% | \$14,922 | \$2,220 | \$2,511 |
| 2016 | 9% | 8% | 25% | 88% | \$14,788 | \$1,476 | \$2,577 | |