Enrolled Actuaries Basic Examination

EA-1

Date: Tuesday, May 5, 2015
Time: 8:30 a.m. – 11:00 a.m.

INSTRUCTIONS TO CANDIDATES

1. Write your candidate number here ____________. Your name must not appear.
2. Do not break the seal of this book until the supervisor tells you to do so.
3. Special conditions generally applicable to all questions on this examination are found at the front of this book.
4. On this examination the symbol “\(a\)” will be used to represent the number of lives at age \(x\).
5. This examination consists of 31 multiple-choice questions worth a total of 100 points. The point value for each question is shown in parentheses at the beginning of the question.
6. Your score will be based on the point values of questions that you answer correctly. No credit will be given for omitted answers and no credit will be lost for wrong answers; hence, you should answer all questions even those for which you have to guess.
7. A separate answer sheet is inside the front cover of this book. During the time allotted for this examination, record all your answers on side 2 of the answer sheet. NO ADDITIONAL TIME WILL BE ALLOWED FOR THIS PURPOSE. No credit will be given for anything indicated in the examination book but not transferred to the answer sheet. Failure to stop writing or coding your answer sheet after time is called will result in the disqualification of your answer sheet or further disciplinary action.
8. Five answer choices are given with each question, each answer choice being identified by a key letter (A to E). For each question, blacken the oval on the answer sheet that corresponds to the key letter of the answer choice that you select.
9. Use a soft-lead pencil to mark the answer sheet. To facilitate correct mechanical scoring, be sure that, for each question, your pencil mark is dark and completely fills only the intended oval. Make no stray marks on the answer sheet. If you have to erase, do so completely.
10. Do not spend too much time on any one question. If a question seems too difficult, leave it and go on.
11. While every attempt is made to avoid defective questions, sometimes they do occur. If you believe a question is defective, the supervisor or proctor cannot give you any guidance beyond the instructions on the exam booklet.
12. Clearly indicated answer choices in the test book can be an aid in grading examinations in the unlikely event of a lost answer sheet.
13. Use the blank portions of each page for your scratch work. Extra blank pages are provided at the back of the examination book.
14. When the supervisor tells you to do so, break the seal on the book and remove the answer sheet.

On the front of the answer sheet, space is provided to write and code candidate information. Complete the information requested by printing in the squares and blackening the circles (one in each column) corresponding to the letters or numbers printed. For each empty box blacken the small circle immediately above the “A” circle. Fill out the boxes titled:

(a) Name
   (Include last name, first name and middle initial)
(b) Candidate Number
   (Candidate/Eligibility Number, use leading zeros if needed to make it a five digit number)
(c) Test Site Code
   (The supervisor will supply the number.)
(d) Examination Part
   (Code the examination that you are taking by blackening the circle to the left of “Exam EA-1”)
(e) Booklet Number
   (The booklet number can be found in the upper right-hand corner of this examination book. Use leading zeros if needed to make it a four digit number.)

In the box titled “Complete this section only if instructed to do so”, fill in the circle to indicate if you are using a calculator and write in the make and model number.

In the box titled “Signature and Date” sign your name and write today’s date. **If the answer sheet is not signed, it will not be graded.**

Leave the boxes titled “Test Code” and “Form Code” blank.

On the back of the answer sheet fill in the Booklet Number in the space provided.

15. After the examination, the supervisor will collect this book and the answer sheet separately. **DO NOT ENCLOSE THE ANSWER SHEET IN THE BOOK.** All books and answer sheets must be returned. THE QUESTIONS ARE CONFIDENTIAL AND MAY NOT BE TAKEN FROM THE EXAMINATION ROOM.
<table>
<thead>
<tr>
<th>Question</th>
<th>Answer</th>
<th>Question</th>
<th>Answer</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>D</td>
<td>26</td>
<td>E</td>
</tr>
<tr>
<td>2</td>
<td>E</td>
<td>27</td>
<td>D</td>
</tr>
<tr>
<td>3</td>
<td>E</td>
<td>28</td>
<td>B</td>
</tr>
<tr>
<td>4</td>
<td>B</td>
<td>29</td>
<td>C</td>
</tr>
<tr>
<td>5</td>
<td>B</td>
<td>30</td>
<td>C</td>
</tr>
<tr>
<td>6</td>
<td>E</td>
<td>31</td>
<td>C</td>
</tr>
<tr>
<td>7</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>A</td>
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<tr>
<td>10</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>E</td>
<td></td>
<td></td>
</tr>
<tr>
<td>14</td>
<td>D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>E</td>
<td></td>
<td></td>
</tr>
<tr>
<td>16</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>18</td>
<td>E</td>
<td></td>
<td></td>
</tr>
<tr>
<td>19</td>
<td>D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>21</td>
<td>C</td>
<td></td>
<td></td>
</tr>
<tr>
<td>22</td>
<td>D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>23</td>
<td>A</td>
<td></td>
<td></td>
</tr>
<tr>
<td>24</td>
<td>B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>25</td>
<td>B</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
If applicable, the following conditions should be considered a part of the data for each question, unless otherwise stated or implied:

(1) The normal retirement age is 65.

(2) Retirement pensions commence at normal retirement age and are paid monthly for life at the beginning of each month.

(3) There are no pre-retirement death or disability benefits.

(4) Actuarial equivalence is based on the mortality table and interest rate assumed for funding purposes.

(5) Interest rates that are compounded more frequently than annually are expressed as nominal rates.

(6) Where multiple lives are involved, future lifetimes are assumed to be independent of each other.

(7) The term “gross single premium” is equivalent to “contract single premium;” the term “net single premium” is equivalent to “single benefit premium;” the term “gross annual premium” is equivalent to “annual contract premium;” the term “net annual premium” is equivalent to “annual benefit premium.”

(8) There are no policy loans in effect.

(9) For a bond, the face amount and the redemption value are the same.

(10) Interest rate equals yield rate.

(11) The term “duration” means “Macaulay duration.”
Data for Question 1 (2 points)

\[
\frac{i^{(12)}}{d^{(12)}} = 1.01
\]

Question 1

In what range is the annual rate of interest compounded annually?

(A) Less than 12.2%

(B) 12.2% but less than 12.4%

(C) 12.4% but less than 12.6%

(D) 12.6% but less than 12.8%

(E) 12.8% or more
Data for Question 2 (3 points)

You are given the following at 3.0% interest, compounded annually:

<table>
<thead>
<tr>
<th>$x$</th>
<th>$N_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>88</td>
<td>208</td>
</tr>
<tr>
<td>89</td>
<td>153</td>
</tr>
<tr>
<td>90</td>
<td>110</td>
</tr>
<tr>
<td>91</td>
<td>77</td>
</tr>
<tr>
<td>92</td>
<td>53</td>
</tr>
<tr>
<td>93</td>
<td>35</td>
</tr>
</tbody>
</table>

Question 2

In what range is $\frac{Q_{89}}{T}$?

(A) Less than 0.47
(B) 0.47 but less than 0.49
(C) 0.49 but less than 0.51
(D) 0.51 but less than 0.53
(E) 0.53 or more
Data for Question 3 (3 points)

\[
\begin{align*}
10 E_x &= 0.400 \\
10 a_x &= 7.000 \\
\dot{s}_{x:10} &= 15.000 \\
\end{align*}
\]

Question 3

In what range is \( \bar{a}_x \)?

(A) Less than 12.70

(B) 12.70 but less than 12.90

(C) 12.90 but less than 13.10

(D) 13.10 but less than 13.30

(E) 13.30 or more
Data for Question 4 (3 points)

On 1/1/2015, an endowment fund is established to provide scholarships.

The fund provides for 1 scholarship at the end of year one, 2 scholarships at the end of year two, and so forth up to 10 scholarships in year ten and each year thereafter.

Amount of each scholarship: $25,000.

Interest rate: 5.0% per year, compounded annually.

$X = \text{The value on 1/1/2015 of the endowment fund.}$

Question 4

In what range is X?

(A) Less than $4,000,000

(B) $4,000,000, but less than $4,100,000

(C) $4,100,000, but less than $4,200,000

(D) $4,200,000, but less than $4,300,000

(E) $4,300,000 or more
Data for Question 5 (4 points)

A 25-year bond has 5.5% annual coupons, and is purchased and redeemable at par.

$X = $ the duration of the bond.

Question 5

In what range is $X$?

(A) Less than 14.0
(B) 14.0 but less than 14.5
(C) 14.5 but less than 15.0
(D) 15.0 but less than 15.5
(E) 15.5 or more
Data for Question 6 (2 points)

The following values are from a life table:

<table>
<thead>
<tr>
<th>$x$</th>
<th>$l_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>56</td>
<td>8,223,010</td>
</tr>
<tr>
<td>57</td>
<td>8,106,161</td>
</tr>
<tr>
<td>58</td>
<td>7,980,191</td>
</tr>
<tr>
<td>59</td>
<td>7,844,525</td>
</tr>
<tr>
<td>60</td>
<td>7,698,698</td>
</tr>
<tr>
<td>61</td>
<td>7,542,106</td>
</tr>
<tr>
<td>62</td>
<td>7,374,370</td>
</tr>
<tr>
<td>63</td>
<td>7,195,099</td>
</tr>
<tr>
<td>64</td>
<td>7,003,925</td>
</tr>
<tr>
<td>65</td>
<td>6,800,531</td>
</tr>
<tr>
<td>66</td>
<td>6,584,614</td>
</tr>
<tr>
<td>67</td>
<td>6,355,865</td>
</tr>
</tbody>
</table>

For valuation purposes, the actuary applies a 2-year setback.

Smith is currently age 58.

$X = \text{the probability that Smith dies after age 65.}$

Question 6

In what range is $X$?

(A) Less than 0.825

(B) 0.825 but less than 0.840

(C) 0.840 but less than 0.855

(D) 0.855 but less than 0.870

(E) 0.870 or more
Data for Question 7 (4 points)

Data from a double-decrement (death and withdrawal) table:

- The absolute rate of death at age 50 is 0.035.
- The probability of withdrawal is 5 times the probability of death at all ages.

Decrement rates are uniformly distributed in their associated single decrement tables.

$X = \text{the absolute rate of withdrawal at age 50.}$

Question 7

In what range is $X$?

(A) Less than 0.162

(B) 0.162 but less than 0.166

(C) 0.166 but less than 0.170

(D) 0.170 but less than 0.174

(E) 0.174 or more
Data for Question 8 (4 points)

Smith (age 65) is eligible to retire with a monthly pension benefit payable under one of the following actuarially equivalent forms of payment:

1. A straight life annuity of $15,000.

2. An annuity of $13,500 payable to Smith, with $6,750 continuing to Smith’s surviving spouse after Smith’s death.

3. An annuity of $X payable to Smith, with 75% of $X continuing to Smith’s surviving spouse after Smith’s death.

All annuity payments are made at the beginning of each month.

Question 8

In what range is $X$?

(A) Less than $12,200

(B) $12,200 but less than $12,500

(C) $12,500 but less than $12,800

(D) $12,800 but less than $13,100

(E) $13,100 or more
Data for Question 9 (2 points)

You are given the following information for a fund:

<table>
<thead>
<tr>
<th>Date</th>
<th>Account Balance</th>
<th>Deposit</th>
</tr>
</thead>
<tbody>
<tr>
<td>1/1/2014</td>
<td>$500,000</td>
<td>$100,000</td>
</tr>
<tr>
<td>8/1/2014</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The dollar-weighted rate of return for 2014 equals 18.46%.

Realized gain for 2014 equals $20,000.

Interest plus dividends for 2014 equals $10,000.

There are no other cash flows during 2014.

\( X \) = the unrealized gain during 2014.

Question 9

In what range is \( X \)?

(A) Less than $75,000

(B) $75,000 but less than $85,000

(C) $85,000 but less than $95,000

(D) $95,000 but less than $105,000

(E) $105,000 or more
Data for Question 10 (4 points)

Smith’s salary on 1/1/2015 is $50,000.

On each subsequent 1/1, Smith’s salary will increase 4.0% over his salary on the prior 1/1.

On each 12/31, beginning 12/31/2015, Smith will deposit 2.0% of his salary into a fund.

The fund earns an annual effective rate of interest of 5.0%.

\( X = \) the accumulated value of Smith’s deposits in the fund as of 1/1/2030.

Question 10

In what range is \( X \)?

(A) Less than $27,000

(B) $27,000 but less than $28,000

(C) $28,000 but less than $29,000

(D) $29,000 but less than $30,000

(E) $30,000 or more
Data for Question 11 (4 points)

Deaths are uniformly distributed over \([0,100]\).

Interest rate: 6.0% per year, compounded annually.

Question 11

In what range is \(100a_{60}\)?

(A) Less than $1,000
(B) $1,000 but less than $1,005
(C) $1,005 but less than $1,010
(D) $1,010 but less than $1,015
(E) $1,015 or more
Data for Question 12 (3 points)

Selected values from a mortality table:

<table>
<thead>
<tr>
<th>x</th>
<th>$e_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>75</td>
<td>10.5</td>
</tr>
<tr>
<td>76</td>
<td>10.0</td>
</tr>
<tr>
<td>77</td>
<td>9.6</td>
</tr>
</tbody>
</table>

$X$ = the number expected to die after age 77 out of 10,000 alive at age 75.

Question 12

In what range is $X$?

(A) Less than 9,000
(B) 9,000 but less than 9,010
(C) 9,010 but less than 9,020
(D) 9,020 but less than 9,030
(E) 9,030 or more
Data for Question 13 (3 points)

Data from a mortality table:

<table>
<thead>
<tr>
<th>$x$</th>
<th>$q_x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>60</td>
<td>0.0156</td>
</tr>
<tr>
<td>61</td>
<td>0.0169</td>
</tr>
<tr>
<td>62</td>
<td>0.0184</td>
</tr>
<tr>
<td>63</td>
<td>0.0201</td>
</tr>
</tbody>
</table>

Interest rate: 5.0% per year, compounded annually.

Question 13

In what range is $\ddot{a}_{60:62:3}$?

(A) Less than 2.450
(B) 2.450 but less than 2.550
(C) 2.550 but less than 2.650
(D) 2.650 but less than 2.750
(E) 2.750 or more
Data for Question 14 (4 points)

Terms of a loan:

- Date of loan: 1/1/2005
- Amount of loan: $100,000
- Term of loan: 360 level monthly repayments
- First repayment date: 2/1/2005
- Interest: 12.0% per year, compounded monthly

Immediately after making the 120th repayment, the borrower decides to add $X to each monthly repayment so that the loan will be repaid after having made a total of 160 monthly repayments.

Question 14

In what range is $X$?

(A) Less than $700
(B) $700 but less than $1,250
(C) $1,250 but less than $1,800
(D) $1,800 but less than $2,350
(E) $2,350 or more
Data for Question 15 (3 points)

Data on a bond:

- **Face amount**: $1,000
- **Term**: 10 years
- **Coupon rate**: 5.0% per year, payable semi-annually

\[ X = \text{Premium if yield to maturity is 4.0\%, compounded annually.} \]

\[ Y = \text{Discount if yield to maturity is 6.0\%, compounded annually.} \]

**Question 15**

In what range is \(|X| - |Y|\)?

(A) Less than $7
(B) $7 but less than $10
(C) $10 but less than $13
(D) $13 but less than $16
(E) $16 or more
Data for Question 16 (4 points)

Smith is currently age 65 and is electing a pension benefit that has the following actuarial equivalent forms of benefit:

Normal form of benefit: $1,500 per month, payable immediately as a single life annuity.

Optional form of benefit: If Smith survives to age 70, a payment of $X per month guaranteed for 5 years, and a single life annuity of $X per month thereafter.

Selected actuarial values:

\[ i = 6.0\% \text{ per year, compounded annually} \]

<table>
<thead>
<tr>
<th>( x )</th>
<th>( D_x )</th>
<th>( N_x )</th>
</tr>
</thead>
<tbody>
<tr>
<td>65</td>
<td>1,000</td>
<td>9,900</td>
</tr>
<tr>
<td>70</td>
<td>730</td>
<td>5,474</td>
</tr>
<tr>
<td>75</td>
<td>400</td>
<td>3,160</td>
</tr>
</tbody>
</table>

Question 16

In what range is \( X \)?

(A) Less than $2,300

(B) $2,300 but less than $2,320

(C) $2,320 but less than $2,340

(D) $2,340 but less than $2,360

(E) $2,360 or more
USE THIS PAGE FOR YOUR SCRATCH WORK

EXTRA BLANK PAPER IS PROVIDED AT THE END OF THE EXAM BOOK
Data for Question 17 (3 points)

A whole life insurance policy purchased by a 60-year old provides a death benefit of $1,000 payable at the end of the year of death.

Selected actuarial values:

\[
i = 6.0\% \text{ per year, compounded annually}
\]

\[
a_{61} = 11.5069
\]

\[
q_{60} = 0.004803
\]

\[X= \text{the net single premium for this policy.}\]

Question 17

In what range is \(X\)?

(A) Less than $255

(B) $255 but less than $285

(C) $285 but less than $315

(D) $315 but less than $345

(E) $345 or more
Data for Question 18 (4 points)

An asset portfolio includes the following zero-coupon bonds at the beginning of a year:

<table>
<thead>
<tr>
<th>Years to maturity</th>
<th>Face amount</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>$10,000</td>
</tr>
<tr>
<td>5</td>
<td>$20,000</td>
</tr>
<tr>
<td>7</td>
<td>$30,000</td>
</tr>
</tbody>
</table>

The term structure of interest rates is:

<table>
<thead>
<tr>
<th>Length of investment</th>
<th>Beginning of year</th>
<th>End of year</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 year</td>
<td>3.00%</td>
<td>0.50%</td>
</tr>
<tr>
<td>2 years</td>
<td>2.75%</td>
<td>0.75%</td>
</tr>
<tr>
<td>3 years</td>
<td>2.75%</td>
<td>1.00%</td>
</tr>
<tr>
<td>4 years</td>
<td>3.00%</td>
<td>1.25%</td>
</tr>
<tr>
<td>5 years</td>
<td>3.25%</td>
<td>1.75%</td>
</tr>
<tr>
<td>6 years</td>
<td>3.25%</td>
<td>1.75%</td>
</tr>
<tr>
<td>7 years</td>
<td>3.50%</td>
<td>2.00%</td>
</tr>
</tbody>
</table>

No zero-coupon bonds are sold or purchased during the year.

\(X\) = the change in the market value of the zero-coupon bonds during the year.

**Question 18**

In what range is \(X\)?

(A) Less than $3,000
(B) $3,000 but less than $4,000
(C) $4,000 but less than $5,000
(D) $5,000 but less than $6,000
(E) $6,000 or more
Data for Question 19 (3 points)

Data from a select and ultimate mortality table:

<table>
<thead>
<tr>
<th>n</th>
<th>$q_{x+n}$ + $q_{x+n}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.05</td>
</tr>
<tr>
<td>1</td>
<td>0.65</td>
</tr>
<tr>
<td>2</td>
<td>0.90</td>
</tr>
<tr>
<td>$\geq 3$</td>
<td>1.00</td>
</tr>
</tbody>
</table>

$l_x = 1000 - 10x, \quad 0 \leq x \leq 100$

$l_{x+3} = l_{x+3}$

$X = l_{68+2}$

Question 19

In what range is $X$?

(A) Less than 294

(B) 294 but less than 296

(C) 296 but less than 298

(D) 298 but less than 300

(E) 300 or more
USE THIS PAGE FOR YOUR SCRATCH WORK

EXTRA BLANK PAPER IS PROVIDED AT THE END OF THE EXAM BOOK

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Data for Question 20 (3 points)

Present values of a monthly joint life annuity of $1, payable at the end of each month:

- If Smith is alive $100
- If Jones is alive $X$
- If only Smith is alive $20$
- If only Smith or only Jones is alive $50$

Question 20

In what range is $X$?

(A) Less than $85$
(B) $85$ but less than $95$
(C) $95$ but less than $105$
(D) $105$ but less than $115$
(E) $115$ or more
Data for Question 21 (2 points)

Selected actuarial values:

\[ l_{x+1} = 960 \]
\[ L_x = 975 \]

Deaths follow uniform distribution between \( x \) and \( x + 1 \).

**Question 21**

In what range is \( 1000m_x \)?

(A) Less than 30.0

(B) 30.0 but less than 30.5

(C) 30.5 but less than 31.0

(D) 31.0 but less than 31.5

(E) 31.5 or more
Data for Question 22 (3 points)

Terms of a loan:

- Repayment period: 10 years
- Payments: Annual payments, payable at the end of each year
  The principal portion of the payment at the end of the $t^{th}$ year is $100t$, $t = 1, 2, 3, \ldots, 10$
- Interest rate: 4.0% per year, compounded annually

$X$ = the present value of the interest portions of the 10 payments at $t = 0$.

Question 22

In what range is $X$?

(A) Less than $950
(B) $950 but less than $1,100
(C) $1,100 but less than $1,250
(D) $1,250 but less than $1,400
(E) $1,400 or more
Data for Question 23 (3 points)

Given the following information:

<table>
<thead>
<tr>
<th>Event</th>
<th>Amount</th>
</tr>
</thead>
<tbody>
<tr>
<td>Account balance as of 1/1/2015</td>
<td>$50,000</td>
</tr>
<tr>
<td>Contribution made 4/1/2015</td>
<td>$4,000</td>
</tr>
<tr>
<td>Withdrawal on 7/1/2016</td>
<td>$7,000</td>
</tr>
<tr>
<td>Account balance as of 10/1/2016</td>
<td>$52,000</td>
</tr>
</tbody>
</table>

\[ X = \text{the annualized rate of return from 1/1/2015 to 10/1/2016 using the dollar-weighted method.} \]

Question 23

In what range is \( X \)?

(A) Less than 6.0%

(B) 6.0% but less than 7.5%

(C) 7.5% but less than 9.0%

(D) 9.0% but less than 10.5%

(E) 10.5% or more
Data for Question 24 (3 points)

Given the following mortality rates as of 1/1/2014:

<table>
<thead>
<tr>
<th>(x)</th>
<th>(q_x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>50</td>
<td>0.0157</td>
</tr>
<tr>
<td>51</td>
<td>0.0167</td>
</tr>
<tr>
<td>52</td>
<td>0.0176</td>
</tr>
<tr>
<td>53</td>
<td>0.0187</td>
</tr>
</tbody>
</table>

It is assumed that rates of mortality decrease by 3.0% per year, compounded annually.

Interest is 5.0% per year, compounded annually.

On 1/1/2024, a 50-year old purchases a $10,000 3-year temporary life annuity, with the first payment at age 50.

\(X\) = the value as of 1/1/2024 of this annuity.

Question 24

In what range is \(X\)?

(A) Less than $28,200
(B) $28,200 but less than $28,400
(C) $28,400 but less than $28,600
(D) $28,600 but less than $28,800
(E) $28,800 or more
Data for Question 25 (4 points)

Given the following:

\[
\begin{align*}
    i & = 5.0\% \text{ per year, compounded annually} \\
    D_{49} & = 6,587.11 \\
    d_{49} & = 790 \\
    1000A_{50} & = 450.426
\end{align*}
\]

Question 25

In what range is \( N_{30} \)?

(A) Less than 70,000
(B) 70,000 but less than 72,500
(C) 72,500 but less than 75,000
(D) 75,000 but less than 77,500
(E) 77,500 or more
Data for Question 26 (4 points)

A perpetuity pays $25,000 at the end of each year.

The effective annual interest rate is 10.0%.

$X$ = the duration of the perpetuity.

Question 26

In what range is $X$?

(A) Less than 9.1

(B) 9.1 but less than 9.6

(C) 9.6 but less than 10.1

(D) 10.1 but less than 10.6

(E) 10.6 or more
USE THIS PAGE FOR YOUR SCRATCH WORK

EXTRA BLANK PAPER IS PROVIDED AT THE END OF THE EXAM BOOK
Data for Question 27 (4 points)

Terms of a bond:

<table>
<thead>
<tr>
<th>Feature</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Face amount</td>
<td>$1,000</td>
</tr>
<tr>
<td>Annual coupons</td>
<td>4.0%</td>
</tr>
<tr>
<td>Term</td>
<td>3 years</td>
</tr>
<tr>
<td>Purchase price</td>
<td>$974.21</td>
</tr>
</tbody>
</table>

The spot rates at the time the bond is issued are:

<table>
<thead>
<tr>
<th>Year</th>
<th>Spot rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.0%</td>
</tr>
<tr>
<td>2</td>
<td>4.0%</td>
</tr>
<tr>
<td>3</td>
<td>Unknown</td>
</tr>
</tbody>
</table>

Future interest rates are the forward interest rates implicit in the initial yield curve.

Immediately after the first coupon payment, the investor sells the bond.

$X =$ the investor’s total realized return on the bond.

Question 27

In what range is $X$?

(A) Less than ($20)

(B) ($20) but less than $0

(C) $0 but less than $20

(D) $20 but less than $40

(E) $40 or more
Data for Question 28 (3 points)

Given the following in a service table:

- Number of active members at exact age 40: 1,500
- Number of voluntary terminations between exact ages 40 and 41: 30
- Number of disability retirements between exact ages 40 and 41: 10
- Number of involuntary terminations between exact ages 40 and 41: 20
- Number of deaths between exact ages 40 and 41: 12

All decrements are uniform over the year of age 40 to 41.

\( X \) = the rate of mortality at age 40 in the associated single decrement table.

Question 28

In what range is \( X \)?

(A) Less than 0.008150
(B) 0.008150 but less than 0.008170
(C) 0.008170 but less than 0.008190
(D) 0.008190 but less than 0.008210
(E) 0.008210 or more
Data for Question 29 (3 points)

Data from a select and ultimate mortality table:

<table>
<thead>
<tr>
<th>x</th>
<th>$q_{[x]}$</th>
<th>$q_{[x]+1}$</th>
<th>$q_{[x]+2}$</th>
<th>$x+2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>71</td>
<td>0.057</td>
<td>0.070</td>
<td>0.082</td>
<td>73</td>
</tr>
<tr>
<td>72</td>
<td>0.060</td>
<td>0.072</td>
<td>0.085</td>
<td>74</td>
</tr>
<tr>
<td>73</td>
<td>0.062</td>
<td>0.075</td>
<td>0.088</td>
<td>75</td>
</tr>
<tr>
<td>74</td>
<td>0.063</td>
<td>0.077</td>
<td>0.090</td>
<td>76</td>
</tr>
</tbody>
</table>

$X = 4q_{[71]+1}$

Question 29

In what range is $X$?

(A) Less than 0.270

(B) 0.270 but less than 0.280

(C) 0.280 but less than 0.290

(D) 0.290 but less than 0.300

(E) 0.300 or more
Data for Question 30 (3 points)

\[ l_x = 100 - x \text{ for } 49 < x \leq 100 \]

\[ i = 4.0\% \text{ per year, compounded annually.} \]

Question 30

In what range is \( N \) ?

(A) Less than 98.0

(B) 98.0 but less than 102.0

(C) 102.0 but less than 106.0

(D) 106.0 but less than 110.0

(E) 110.0 or more
Data for Question 31 (3 points)

Selected actuarial values:

\[ l_{65} = 1,000 \]
\[ l_{65.5} = 975 \]

Deaths are uniformly distributed over each year of age between consecutive integral ages.

Question 31

In what range is \( \mu_{65.4} \) ?

(A) Less than 0.0505

(B) 0.0505 but less than 0.0508

(C) 0.0508 but less than 0.0511

(D) 0.0511 but less than 0.0514

(E) 0.0514 or more

**END OF EXAMINATION**